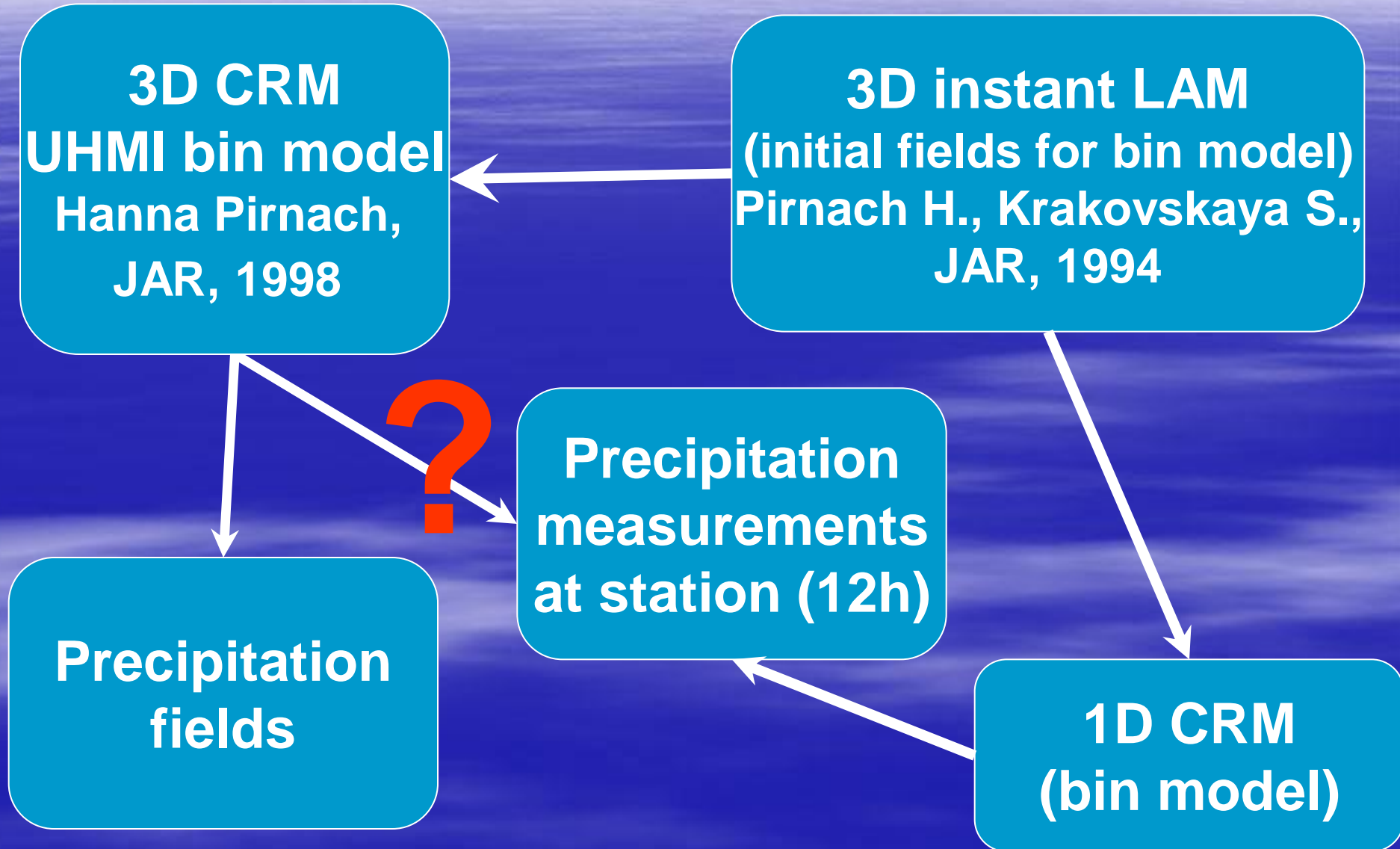


# **Combined Model of Cloudy Troposphere (CMCT) as compromise of Eulerian and Lagrangian approaches**

**Svitlana Krakovska**

*Atmosphere Physics Department  
Ukrainian Hydrometeorological Institute,  
Prospect Nauki 37, Kiev - 03028, Ukraine  
[krasvit@ua.fm](mailto:krasvit@ua.fm)*

# Motivation



# COMBINED MODEL OF CLOUDY TROPOSPHERE (CMCT)

is the combination of 3D time-independent (instant) LAM and 1D CRM with explicit microphysics.

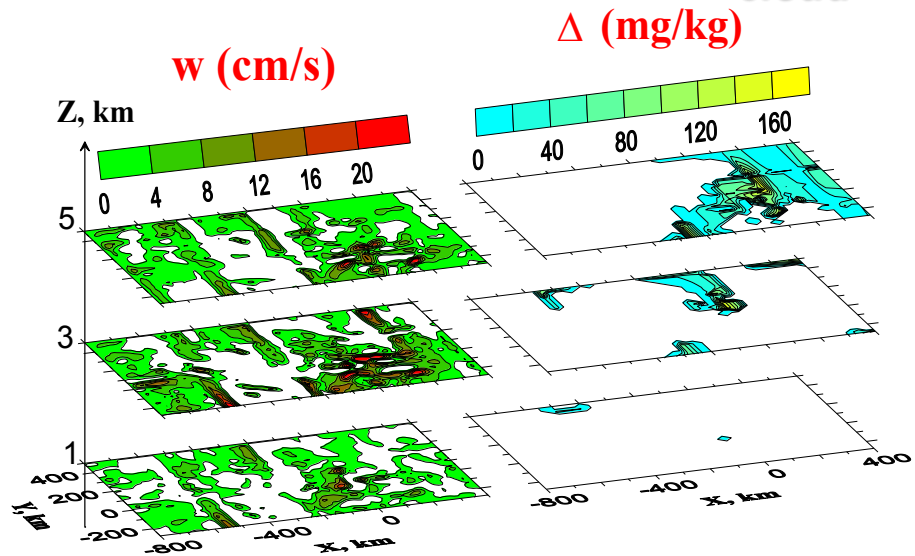
It means that initial thermodynamical characteristics in the vertical column where microphysics is calculated are stepwise updated as it moves along horizontal axes over the initial point of 3D domain  $(X_0, Y_0)$  at every time step  $(dt)$  in 1D model making a track over 3D domain with coordinates

$$X_f = X_0 - \int_0^{t_e} u_f dt \quad Y_f = Y_0 - \int_0^{t_e} v_f dt$$

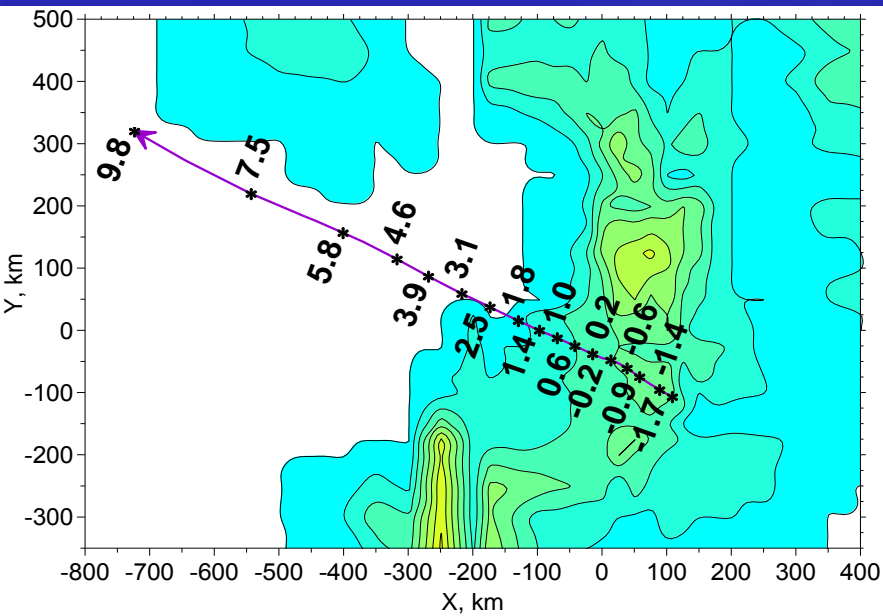
Minus in equations means that the system moves opposite to the air mass displacement. The speed  $u_f, v_f$  of this movement could be constant and determined by synoptic charts or variable and calculated from the data of 3-D LAM, e.g. as an average wind speed in layer up to height  $Z_f$ , or calculated at every vertical level.

# 3-D LAM results with 1-D CRM

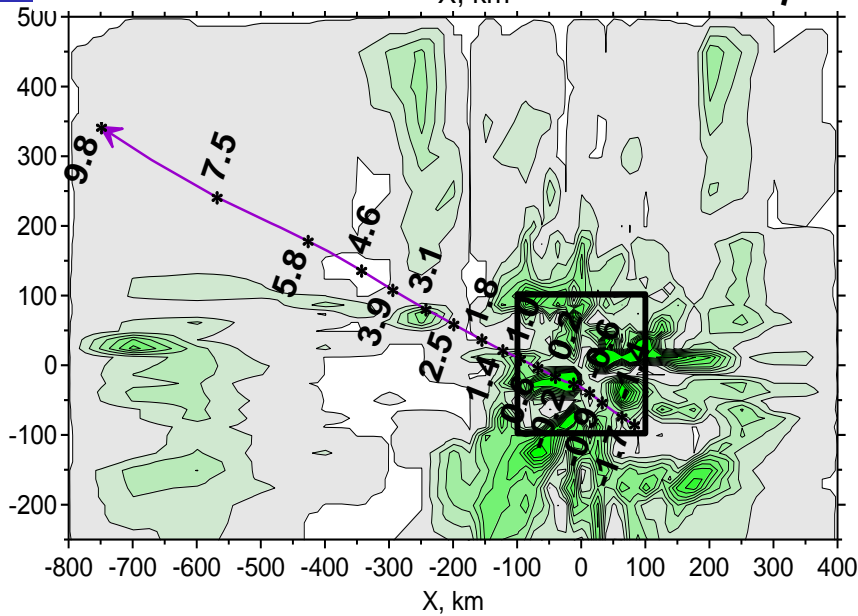
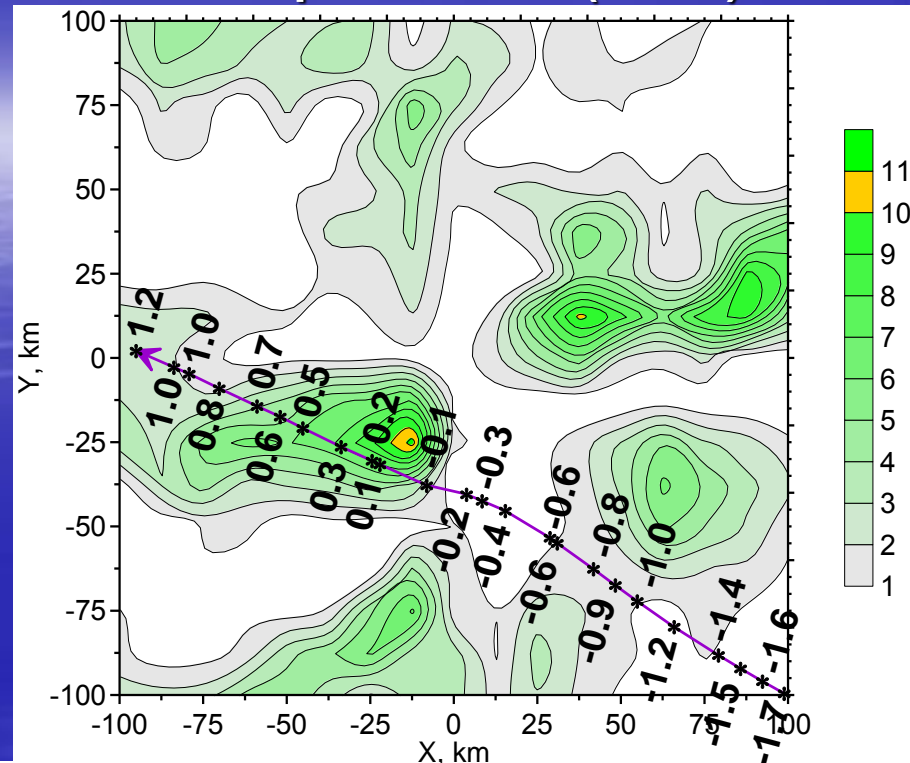
trek (digits near trek -  $t_{cloud}$ , h)



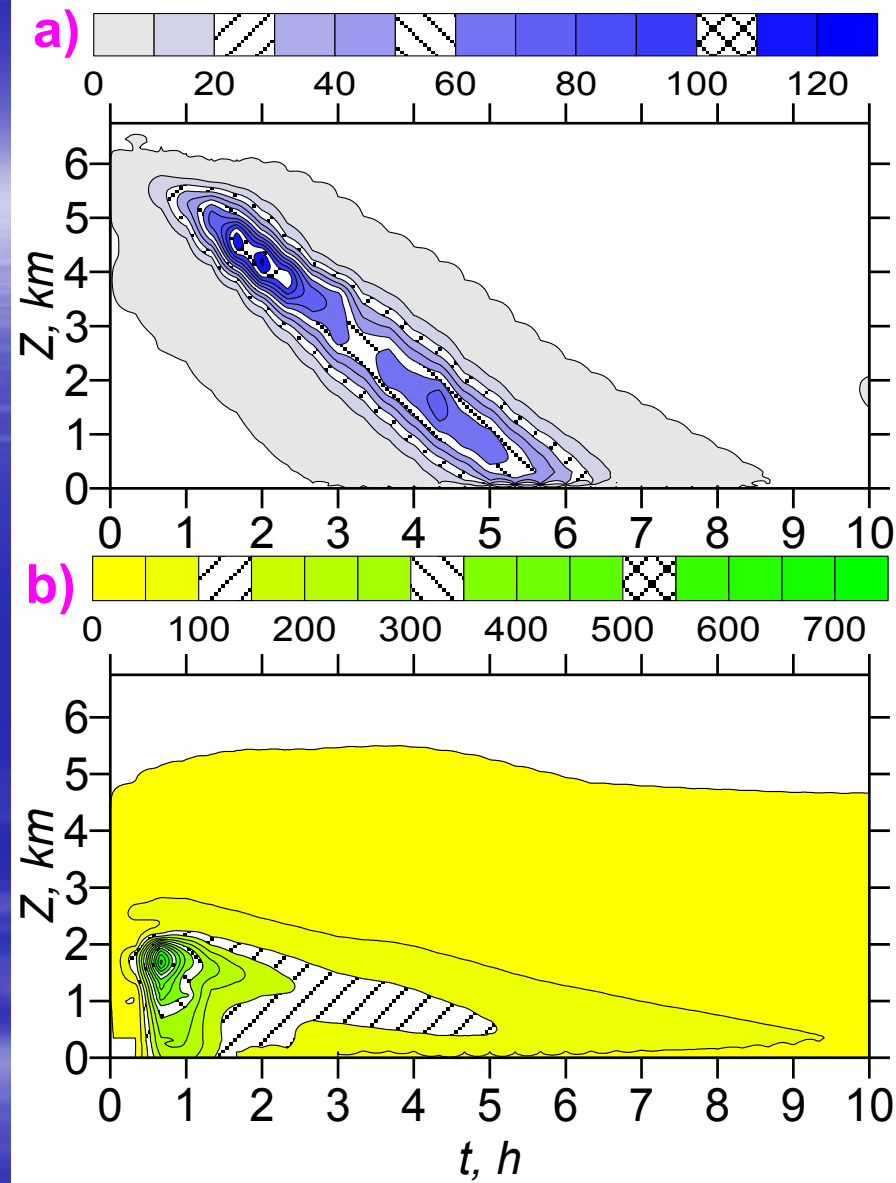
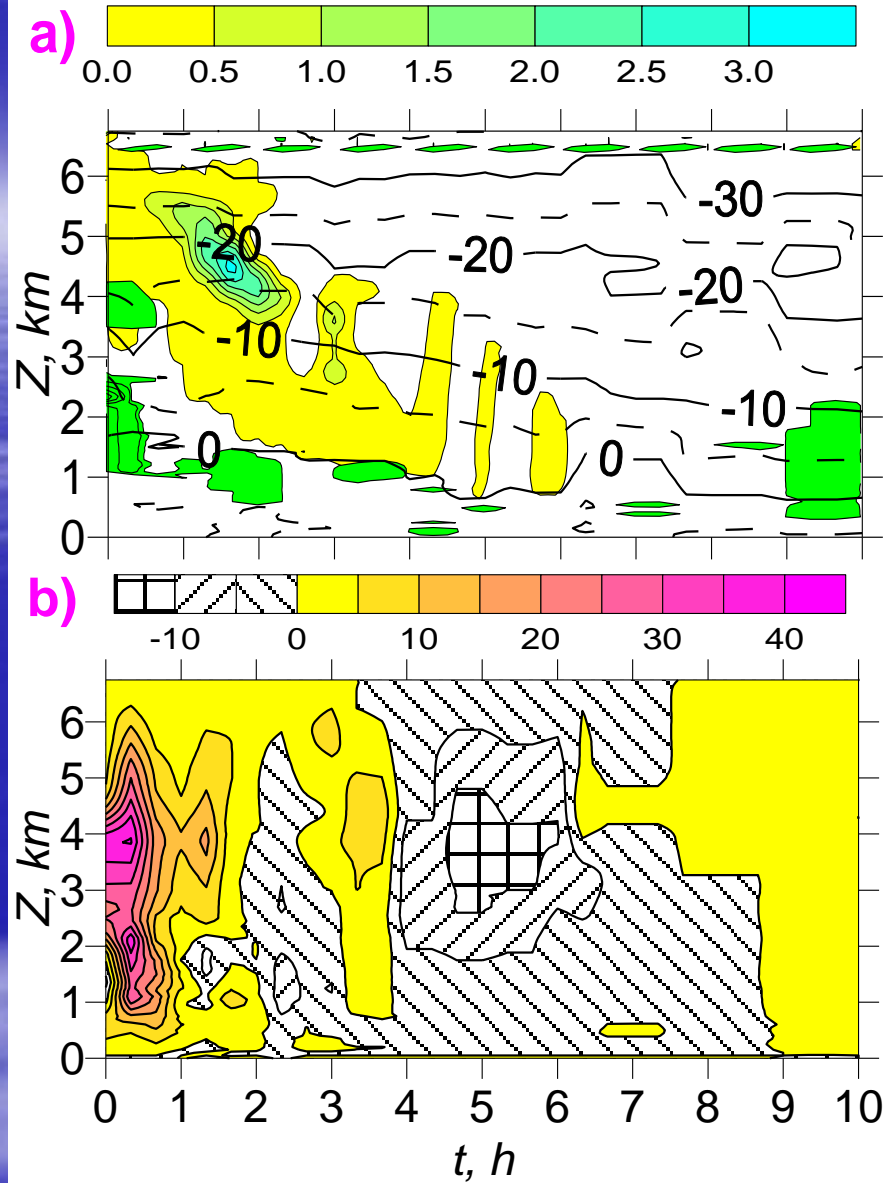
## Integral ice supersaturation (mm)



## Precipitation rate (mm/h)







Initial vertical and time development of:  
 (a) temperature (lines, °C), water (green)  
 and ice supersaturations (shading, mg/kg);  
 (b) vertical motions (cm/s)

Vertical and time development of:  
 (a) IC and (b) LWC (mg/kg)  
 In the run with unmodified freezing

# 1-D SPECTRAL CLOUD RESOLVING MODEL

1. The kinetic equation of cloud droplets ( $k=1$ ) size distribution function ( $f_1$ ):

$$\frac{df_1}{dt} + \frac{\partial}{\partial r} \left( \dot{r}_1 f_1 \right) - v_1 \frac{\partial f_1}{\partial Z} = I_{a1} - I_{f1} - \sigma_2 f_1 - \sigma_3 f_1 + k_z \frac{\partial^2 f_1}{\partial Z^2}$$

2. The kinetic equation of cloud ice crystals ( $k=2$ ) and raindrops ( $k=3$ ) size distribution functions ( $f_k$ ):

$$\frac{df_k}{dt} + \frac{\partial}{\partial r} \left( \dot{r}_k f_k \right) + \frac{\partial}{\partial r} \left( \dot{r}_{ck} f_k \right) - v_k \frac{\partial f_k}{\partial Z} = c_k I_{ak} \pm I_{fk} + k_z \frac{\partial^2 f_k}{\partial Z^2}, \quad c_2 = 1, c_3 = 0$$

3. The equation of heat inflow:

4. The equation of moisture inflow:

$$\frac{dT}{dt} = \sum_{k=1}^3 \alpha_k \varepsilon_k - \gamma_a w + k_z \frac{\partial^2 T}{\partial Z^2}$$

$$\frac{dq}{dt} = - \sum_{k=1}^3 \varepsilon_k + k_z \frac{\partial^2 q}{\partial Z^2}$$

5. The state equation:

$$\rho = \frac{P}{RT}$$

$$\alpha_k = L_k / C_p$$

# 1-D SPECTRAL CLOUD RESOLVING MODEL

Cloud particles generation on CCN is parameterized as follows:

$$I_{\alpha 1} = N_{m0} w \delta(Z - Z_w) \delta(r - r_{10}) \Theta(\Delta_1) + N_c \left( \frac{100 \Delta_1}{q_{s1}} \right)^{K_c} \delta(r - r_{10}) \Theta(\Delta_1 - \Delta_{1w})$$

The rate of growth of individual particles due to condensation (deposition) is:

$$\dot{r}_k = \frac{D \rho \Delta_k}{\Gamma_k \rho_k r} \quad \Gamma_k = 1 + \alpha_k \beta_k, \quad \beta_k = \partial q_{sk} / \partial T$$

and due to gravitational collection of droplets by spherical CP :

$$\dot{r}_{ck} = \frac{\rho_1 \rho \pi}{3 \rho_k r_k^2} \int_{r_{1\min}}^{r_{1\max}} E(r_1, r_k) (r_1 + r_k)^2 (v_k - v_1) r_1^3 f_1(r) dr_1 \quad E(r_1, r_k) = \left[ 1 - \frac{r_k R_0^3}{4 r_1^2 |r_k^2 - r_1^2|} \right]^2$$

$$\sigma_k = \pi \rho \int_{r_{k0}}^{\infty} E(r_1, r_k) (r_1 + r_k)^2 (v_k - v_1) f_k(r) dr_k, \quad k = 2, 3, \quad R_0 = \sqrt[3]{\frac{1,214}{g} \left( \frac{9\eta}{\rho} \right)^2} \approx 14,5 \mu m$$

where  $r_{k0}$  are min radii of CP;  $E(r_1, r_k)$  are coefficients of collection.



# ICE-FORMING PROCESSES IN 1-D CRM

The processes of condensational-depositional freezing on activated IN are parameterized as follows:

$$I_{\alpha 2} = A_s e^{B_s T_s} \frac{dT}{dt} \delta(r - r_{20}) \Theta\left(-\frac{dT}{dt}\right) \Theta(\Delta_1) \Theta(T_s), \quad T_s = T_{\text{lim}} - T$$

The processes of droplets ( $I_{f1}$ ) and raindrops ( $I_{f3}$ ) freezing and the amount of frozen water CP ( $I_{f2}$ ) are parameterized as follows:

$$I_{fk} = A_f e^{B_f T_s} r_k^3 f_k \Theta(T_s) \quad I_{f2} = -(I_{f1} + I_{f3})$$



# INTEGRAL CHARACTERISTICS OF A MIXED CLOUD

Cloud particles concentrations ( $N_k$ ), their average sizes ( $\bar{r}$ ),  
ice and water contents ( $q_k$ ), intensity of precipitation ( $j$ ):

$$N_k = \int_{r_{k \min}}^{r_{k \max}} f_k dr$$

$$q_k = \frac{4\pi\rho_k k_f}{3} \int_{r_{k \min}}^{r_{k \max}} r_k^3 f_k dr_k$$

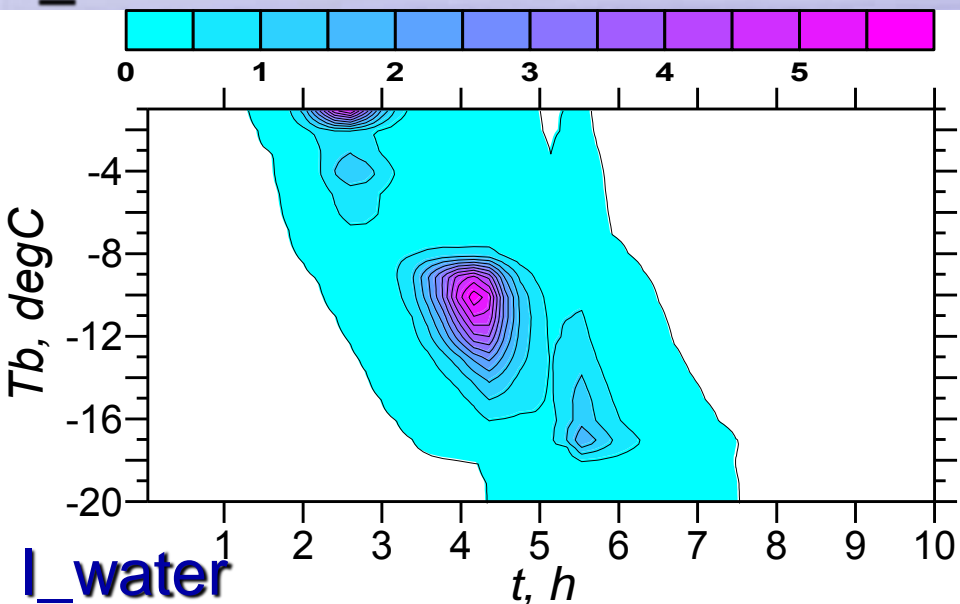
$$N_k \bar{r}_k = \int_{r_{k \min}}^{r_{k \max}} r_k f_k dr$$

$$j = \sum_{k=2}^3 \frac{4\pi\rho_k k_f}{3} \int_{r_{k \min}}^{r_{k \max}} (v_k - w) r_k^3 f_k(r) dr$$

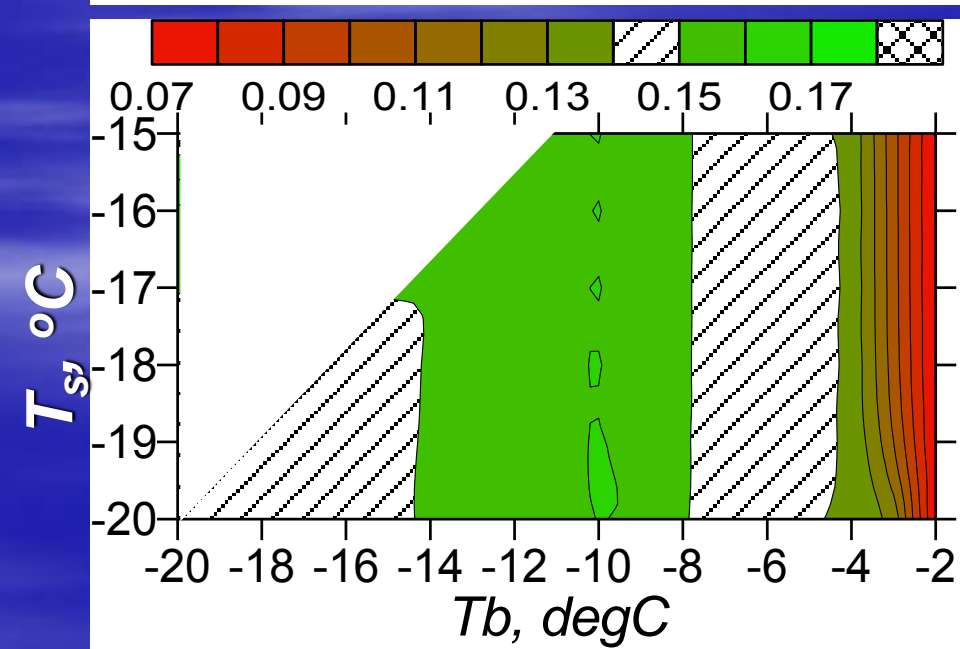
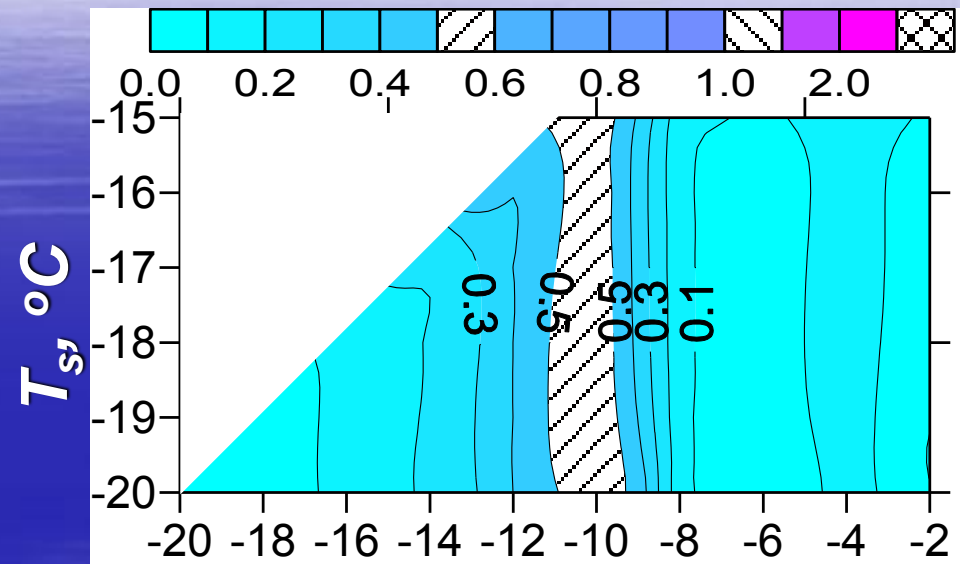
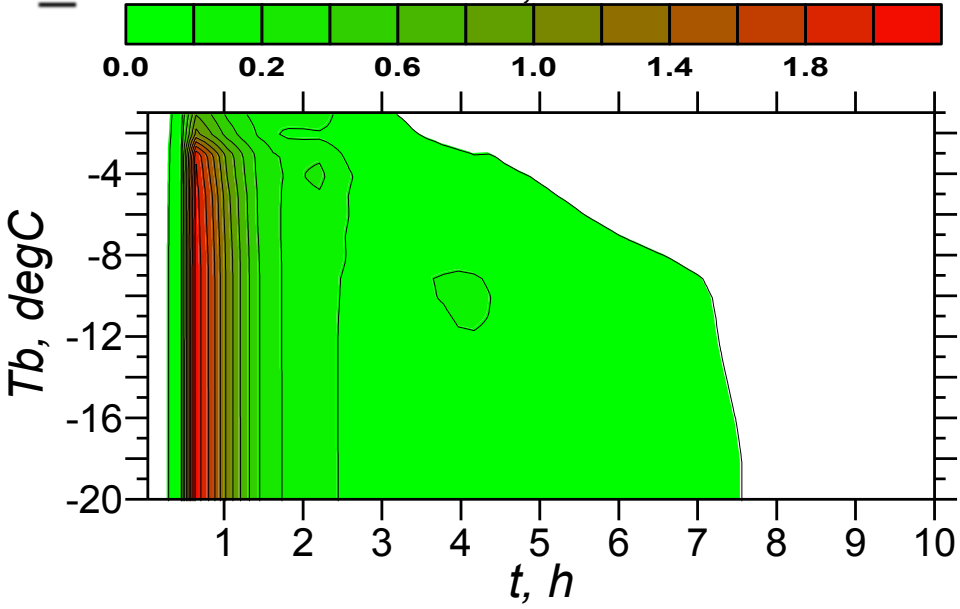
where  $r_{k \min}$  and  $r_{k \max}$  are minimum and maximum radii of CP.

# Precipitation intensity (mm/h) in dependence of $T_s$ and $T_b$ (pseudo-contact freezing)

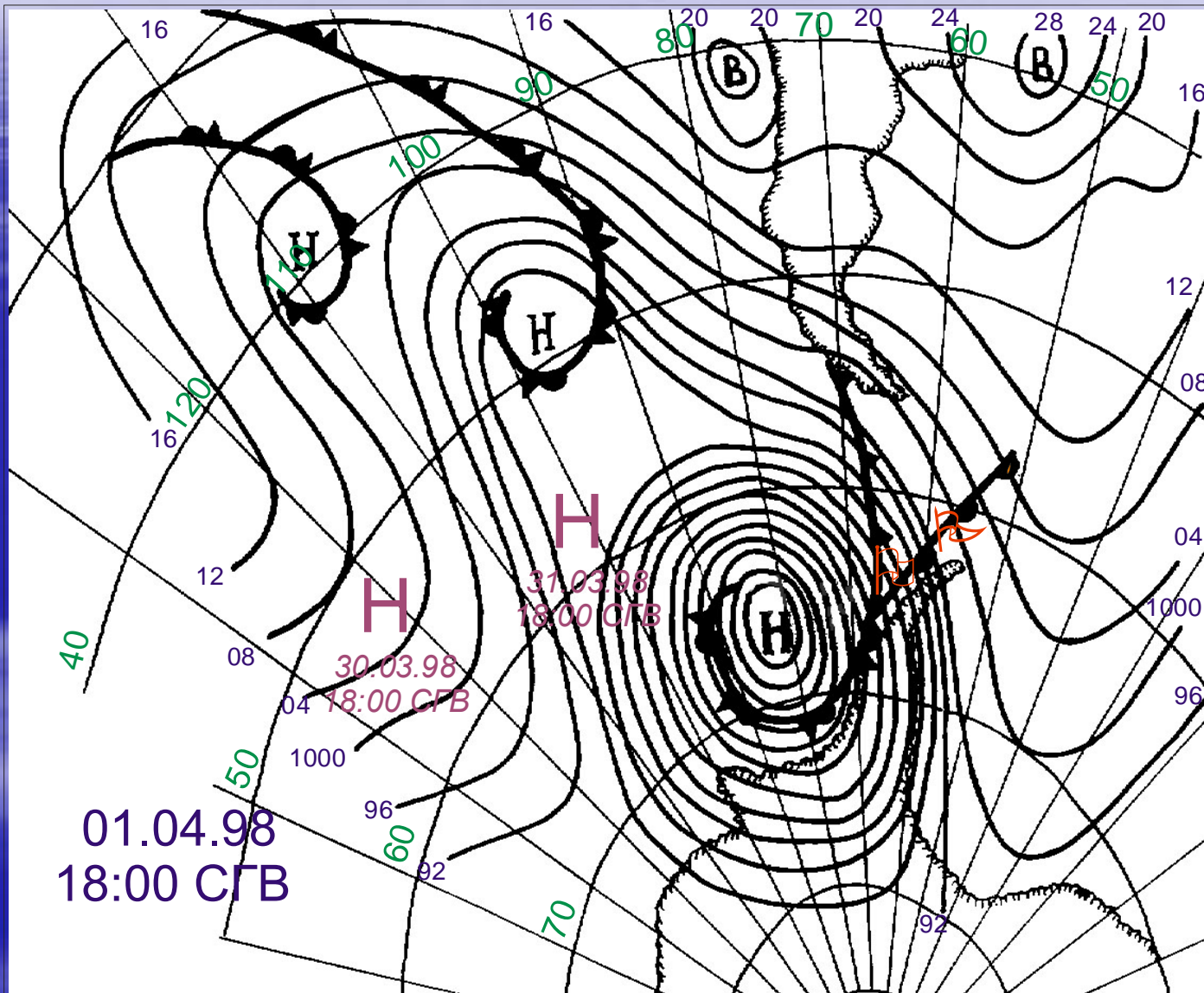
## $I_{ice}$

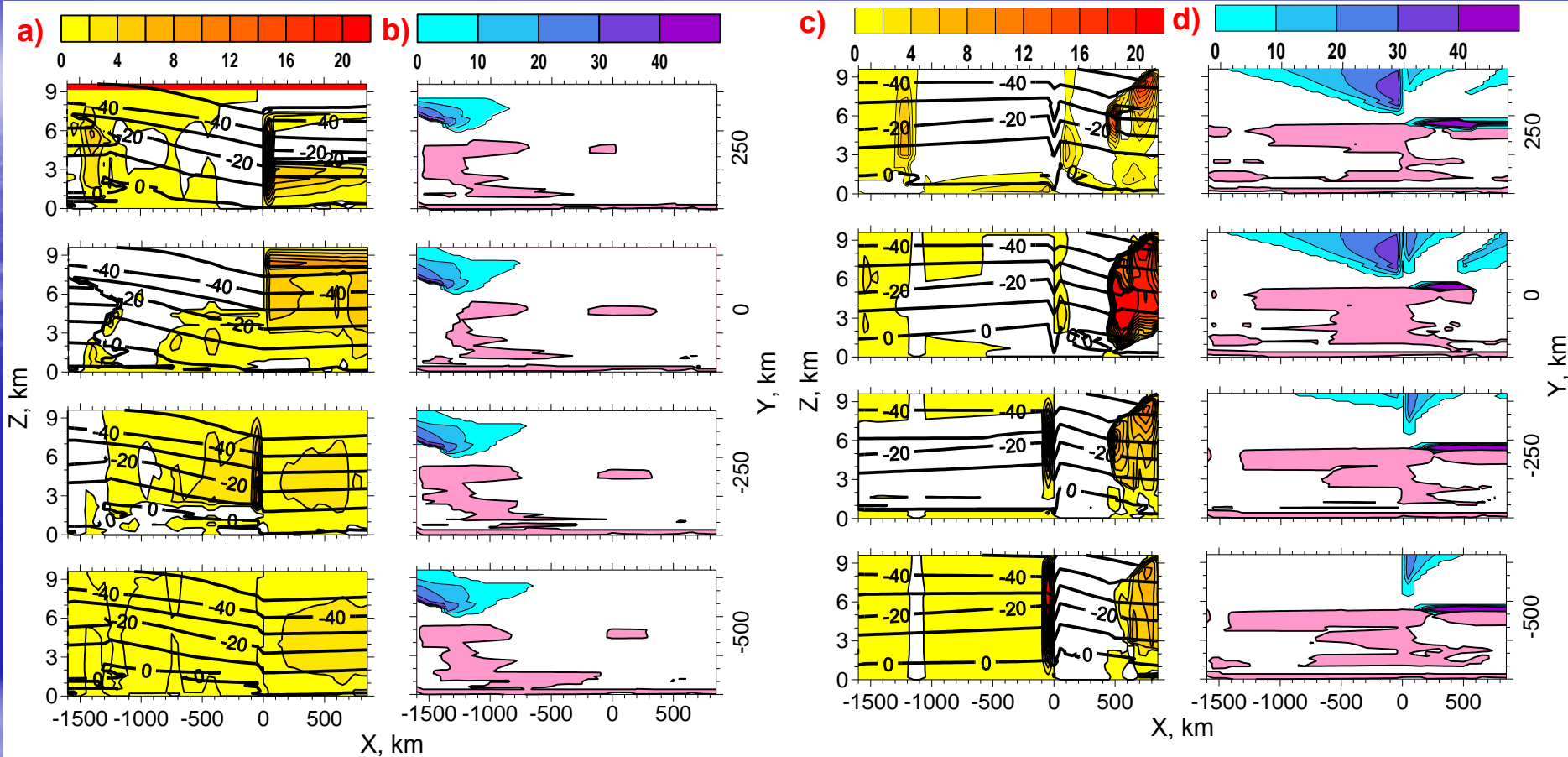


## $I_{water}$



# Synoptic map (H – center of the Low)





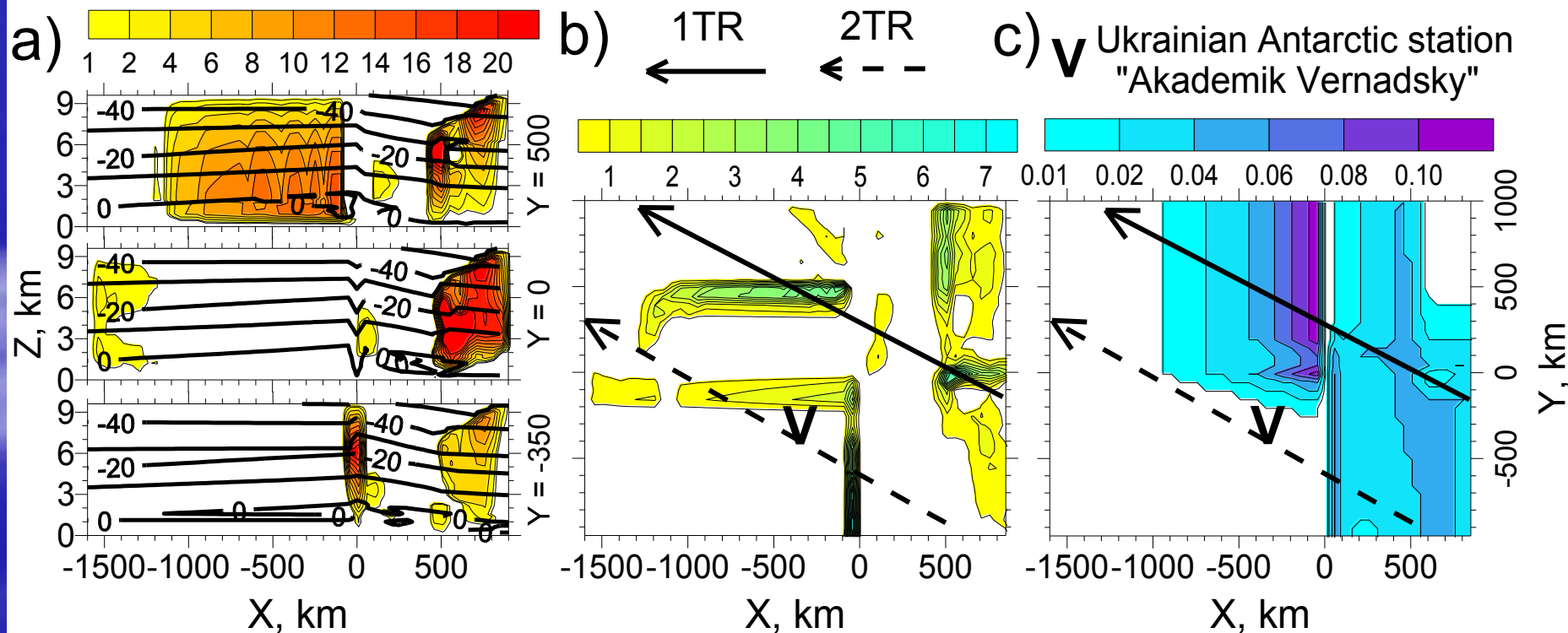
Vertical cross-sections for 00 CГВ 01.04.98 (a, b) and 00 CГВ 02.04.98 (c, d):  
 (a) and (c) temperature (lines with numbers, °C)  
 and up-drafts (yellow-red, cm/s);  
 (b) and (d) ice supersaturation (blue-violet, mg/kg)  
 and wet-instability (pink)



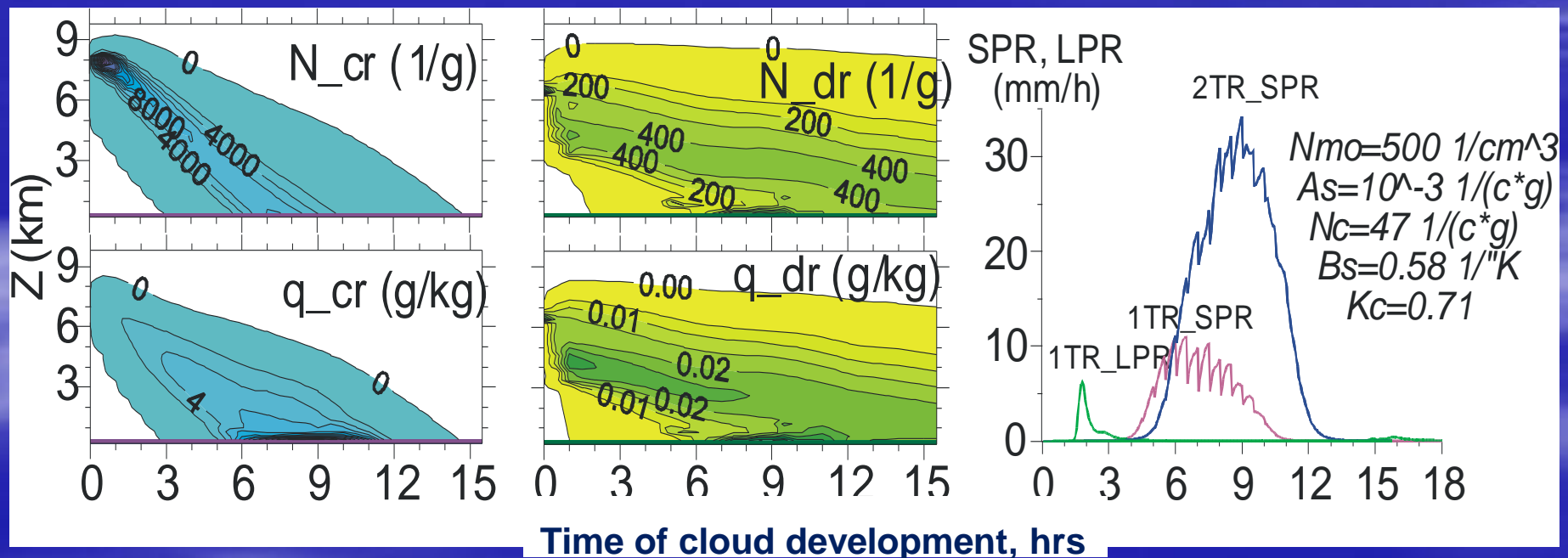
# Results of 3D simulation for 00 UTC 02.04.98:

(a) vertical cross-sections of temperature,  $T$  ( $^{\circ}\text{C}$ ), and updrafts,  $w$  (cm/s), (yellow-red);

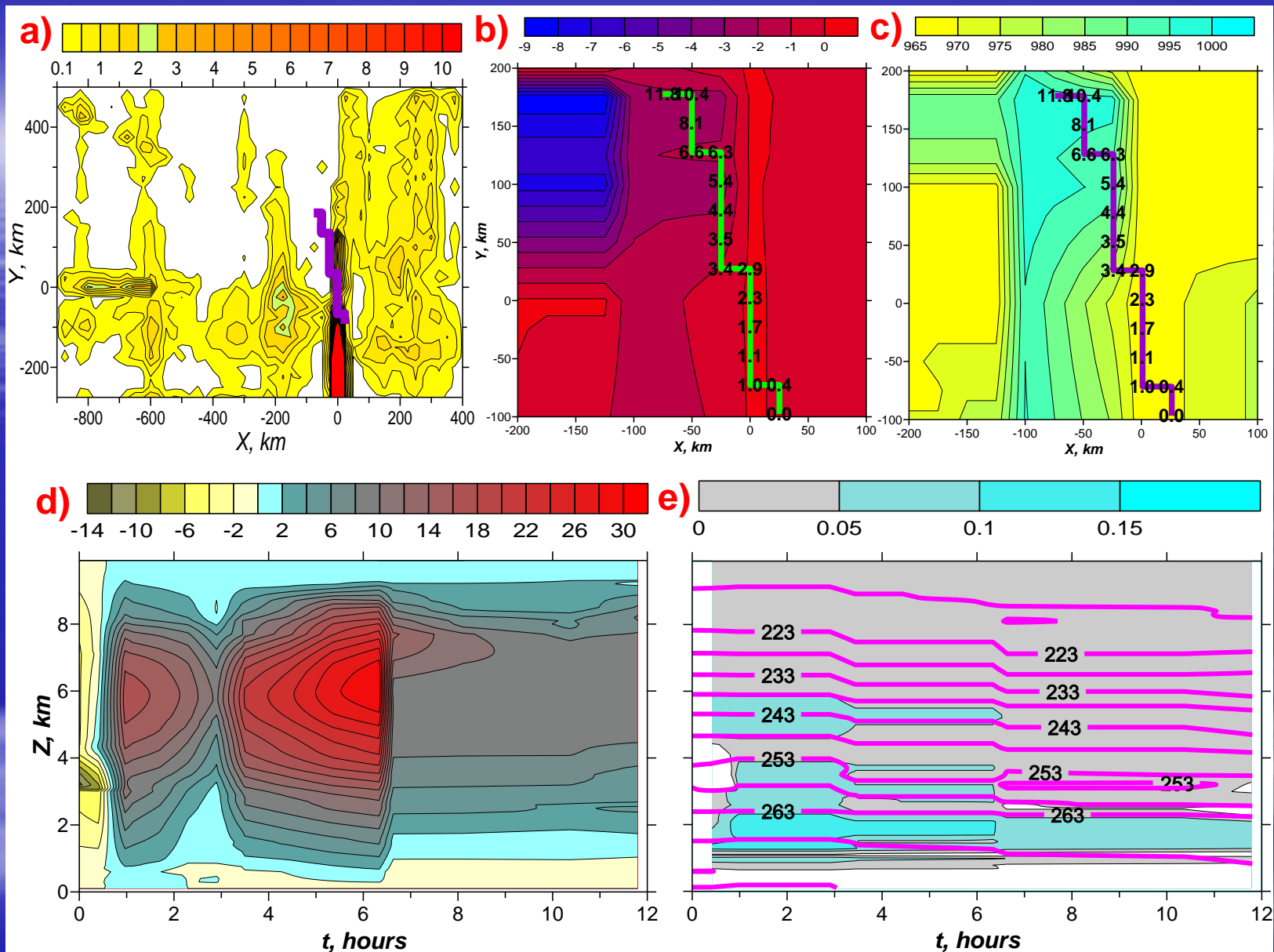
(b) vertically integrated thermodynamic rate of condensation as precipitation rate (mm/h) and (c) ice supersaturation (mm) with treks of 1D bin model



**Integral microphysical characteristics of the cloud  
on the treks (1TR and 2TR) and rates of water  
precipitation (*LPR*) and snow precipitation (*SPR*)  
got in the simulation with pointed initial parameters:  
*N\_cr* and *N\_dr* – ice crystal and drop concentrations,  
*q\_cr* and *q\_dr* – ice and water contents**



Results of the simulation for 20.06.1996  
(central point  $(X, Y) = (0, 0)$  is Bellingshausen station)



(a) integral thermodynamic condensation rate (mm/h), (b) surface temperature ( $^{\circ}\text{C}$ ) and (c) pressure (mb) with a track of the 1D model and vertical development of (d) vertical motions (cm/s), (e) ice supersaturation (mg/kg) and temperature ( $^{\circ}\text{K}$ ) on the track with  $t$

Liquid ( $S_{liq}$ ) and solid ( $S_{sol}$ ) precipitation sums for 12 h with their totals ( $S$ ) in dependence of presence and intensity of cloud and precipitation formation mechanisms (20.06.1996)

$N_{exp}$	$A_s$	$A_f$ for droplets	$A_f$ for drops	$E_{coa}$	$S_{liq\_12h}$ mm	$S_{sol\_12h}$ mm	$S_{12h}$ mm
1	1e-5	2e-3	2e-3	1	0.56	20.99	21.55
2	1e-5	0	0	1	0.57	20.91	21.48
3	1e-5	0	—	0	—	13.66	13.66
4	0	2e-3	—	0	—	13.63	13.63
5	0	2e-3	2e-3	1	2.31	18.18	20.49
6	1e-3	0	—	0	—	15.73	15.73
7	1e-3	2e-3	—	0	—	15.47	15.47
8	1e-3	2e-3	2e-3	1	0.40	34.01	34.41



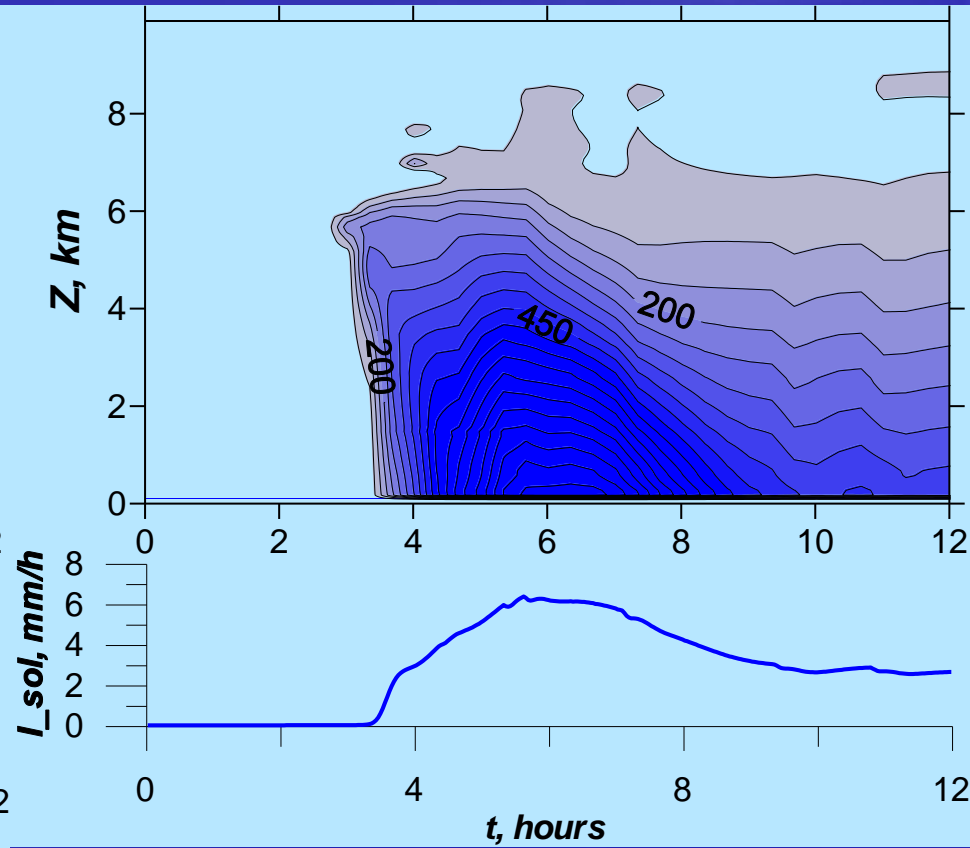
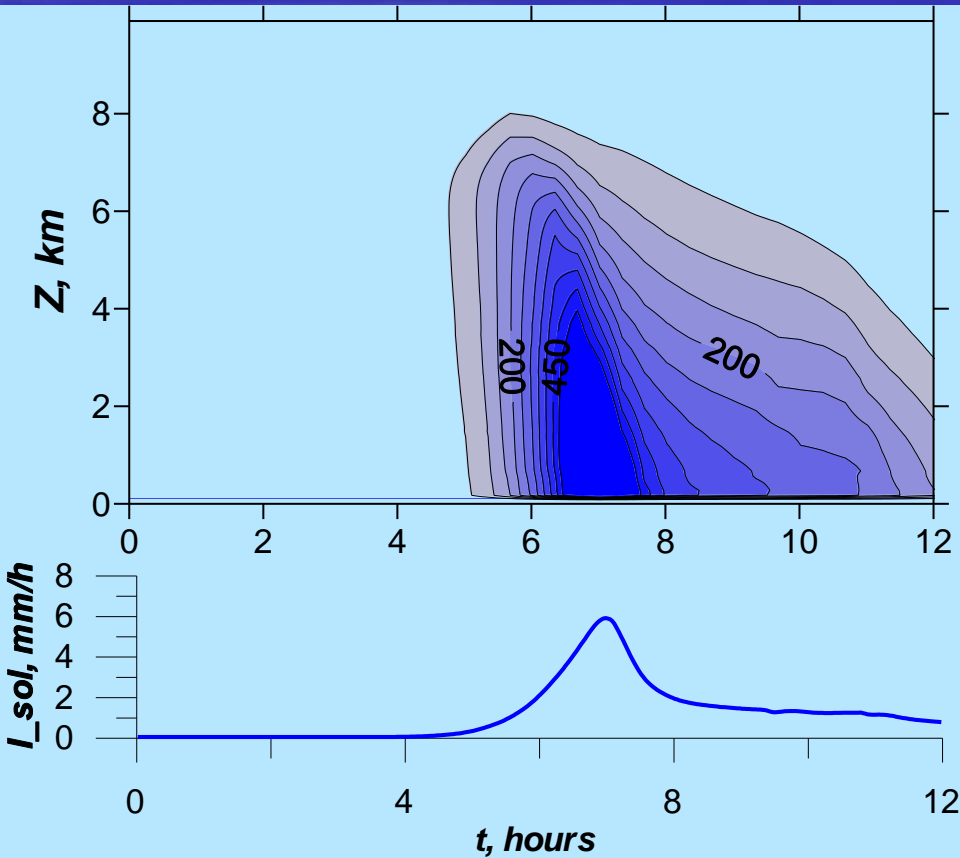
# Ice content (mg/kg)

4

$A_s=0,$   
 $E_{cr}=0, A_f=2e-3$

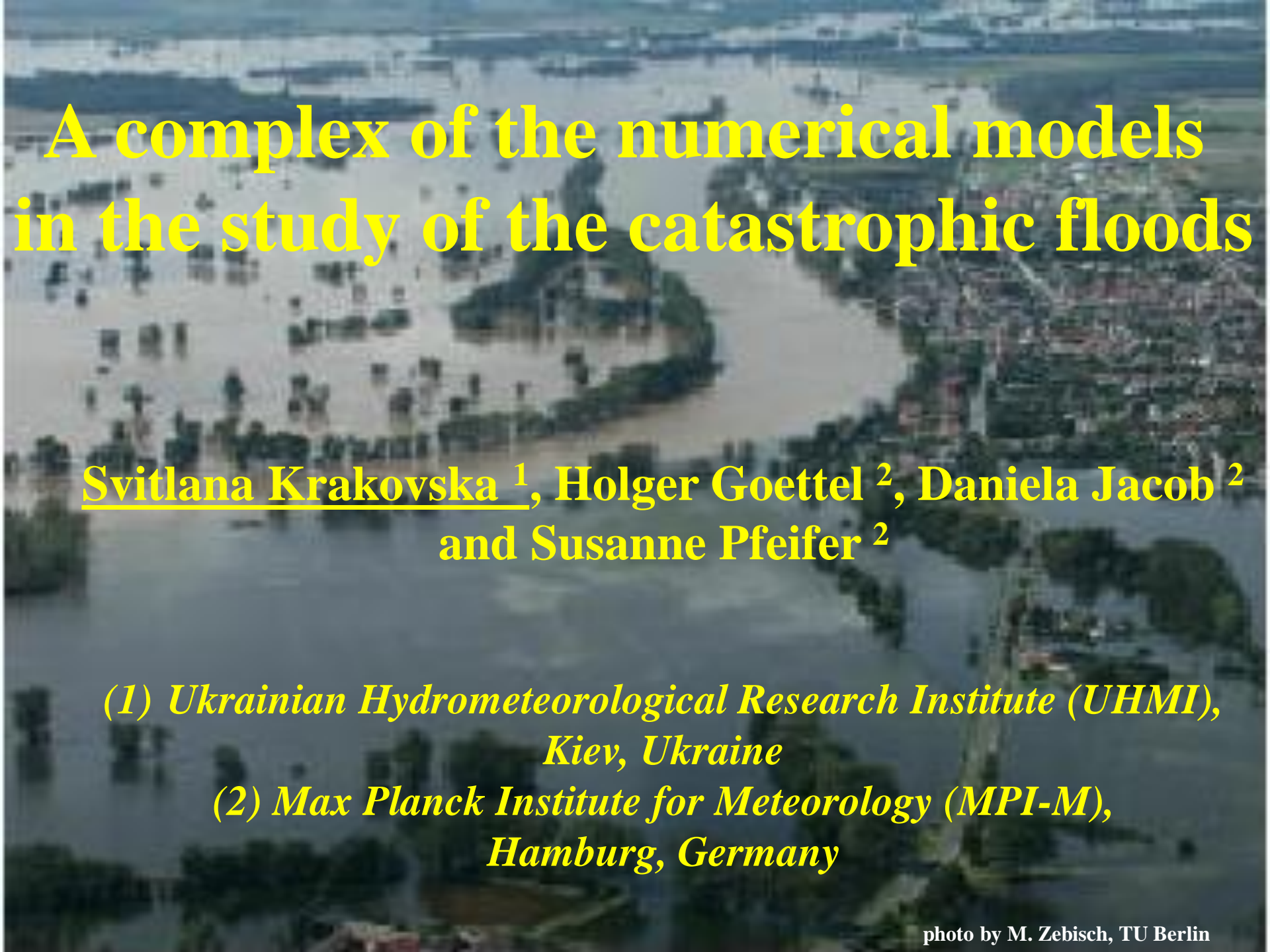
8

$A_s=1e-3,$   
 $E_{cr}=1, A_f=2e-3$



# CONCLUSIONS

- Mixed frontal rainbands over the Antarctic Peninsula were simulated with aid of CMCT and their mesoscale and microphysical features were analyzed.
- The study has confirmed that cloud microphysics obtained in the simulations for Antarctic clouds differ with the microphysical features of midlatitude clouds, particularly ice formation processes dominated and IC exceeded LWC.
- All ice formation processes were almost equally efficient in cloud and precipitation formation.



# **A complex of the numerical models in the study of the catastrophic floods**

**Svitlana Krakovska<sup>1</sup>, Holger Goettel<sup>2</sup>, Daniela Jacob<sup>2</sup>  
and Susanne Pfeifer<sup>2</sup>**

***(1) Ukrainian Hydrometeorological Research Institute (UHMI),  
Kiev, Ukraine***

***(2) Max Planck Institute for Meteorology (MPI-M),  
Hamburg, Germany***



## REMO forecast mode:

driven and initialized by ECMWF T106 Analysis;

initialized every day at 00:00 for 30 hrs simulation with 6 hrs model spin up

horizontal: 109x121 (Elbe case) and 91x91 (Carpathians) grid points

with 1/12° interval;

vertically: 27 levels

The vertical integral ( $E$ ) of **the thermodynamic rate of condensation** in **CMCT** determines development of clouds and corresponds to the possible maximum of precipitation rate:

$$E = - \int_0^H \rho w \frac{\partial q_s}{\partial z} dz$$

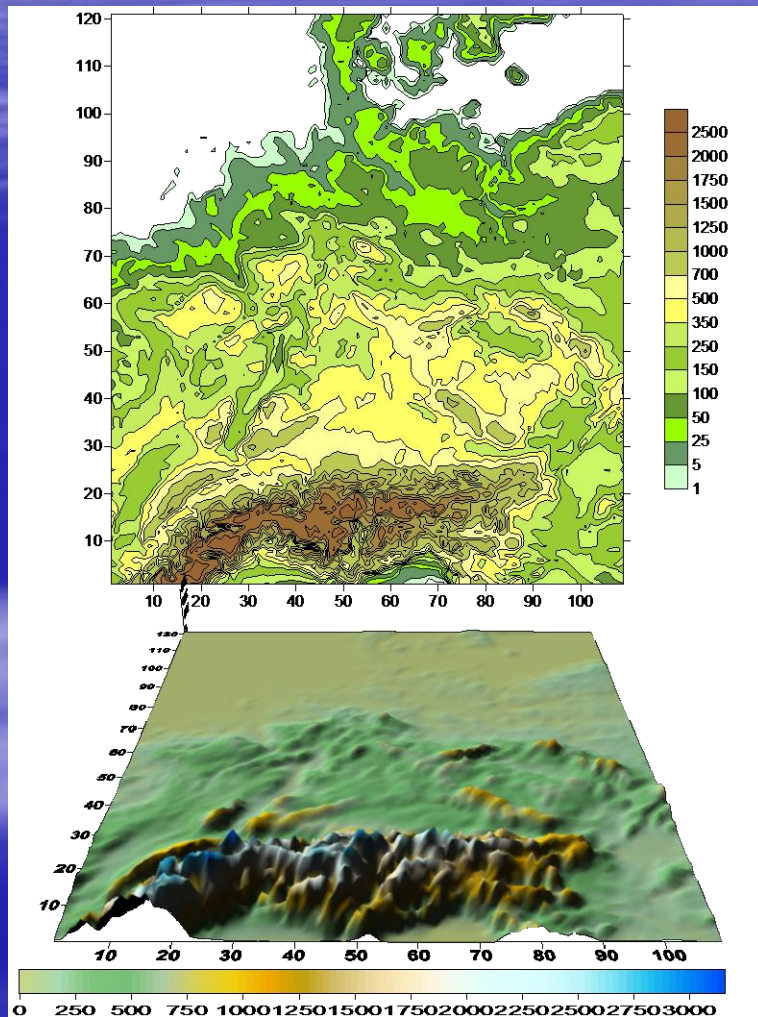
where  $\rho$  and  $q_s$  are the density and specific humidity of the air respectively;  $z$  is the height;  $H$  is the  $z$ -maximum;  $w$  is the vertical component of the wind velocity.



# Models' domains and orography

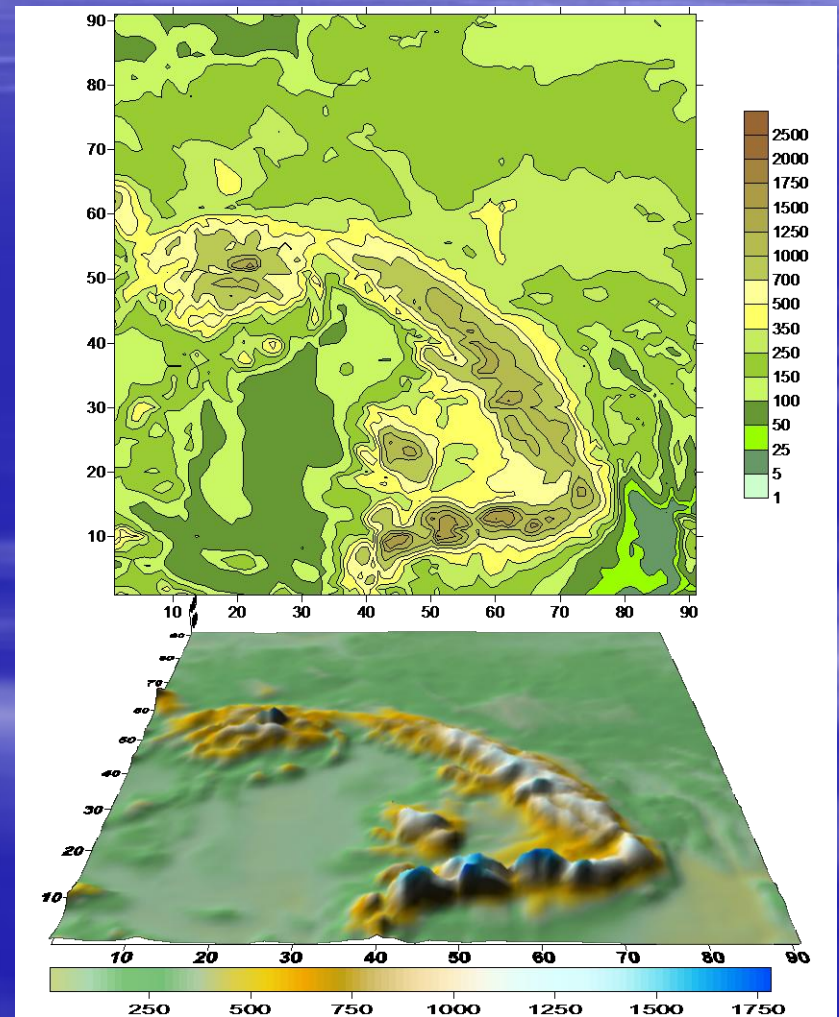
## Elbe case

12-13.08.2002

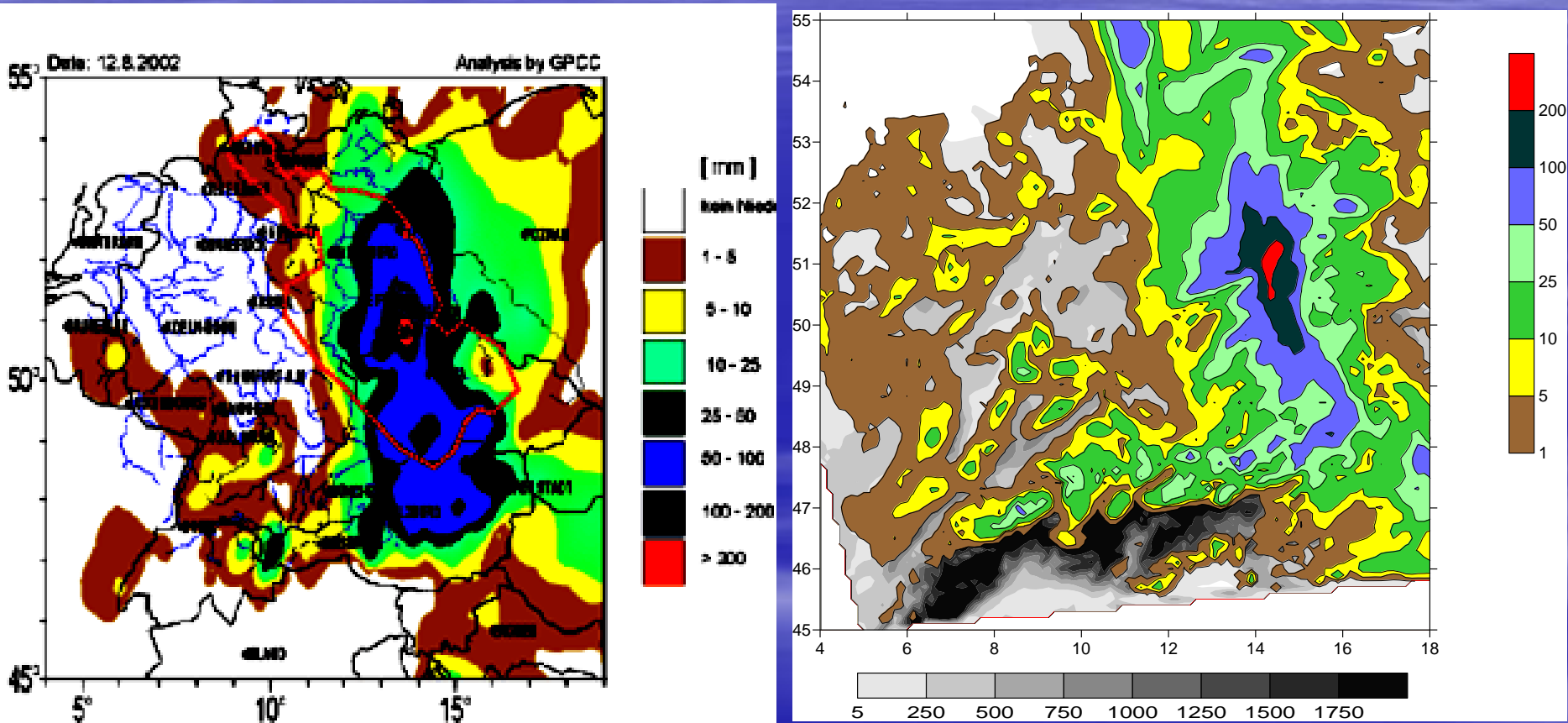


## Carpathians

3-5.11.1998



# Precipitation sum (mm) from GPCC and REMO (117.8 mm) from 07h 12.08.2002 to 06h 13.08.2002



Dresden (13,77°; 51,13°) Daily precip. sum 158 mm

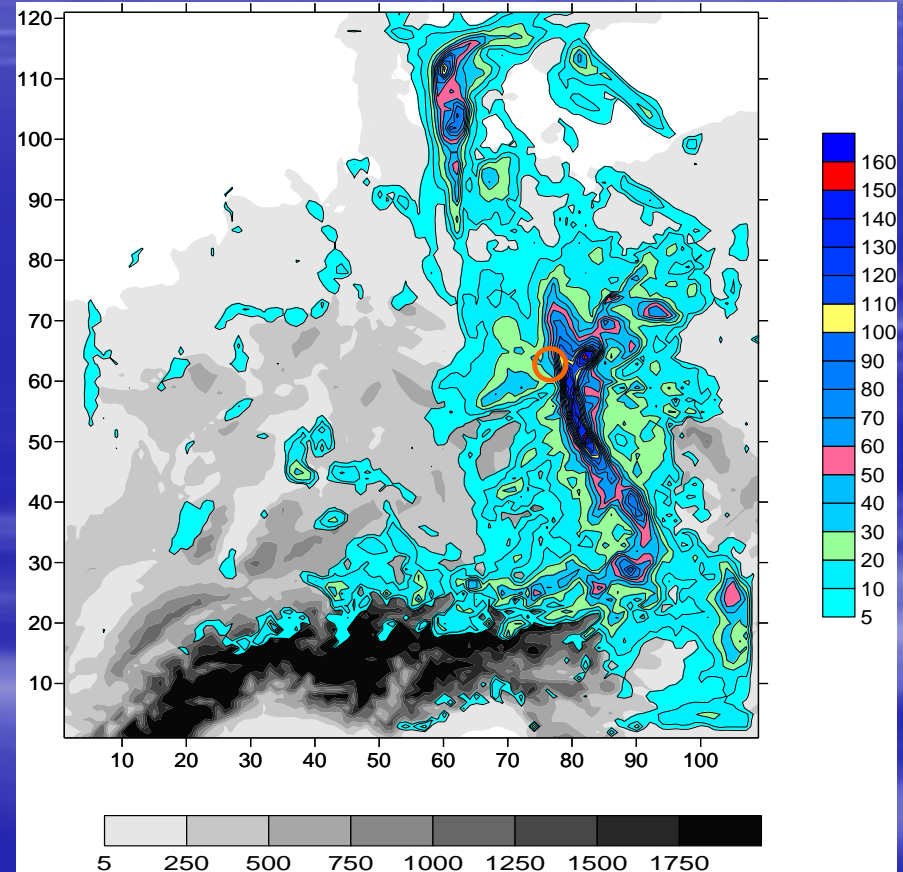
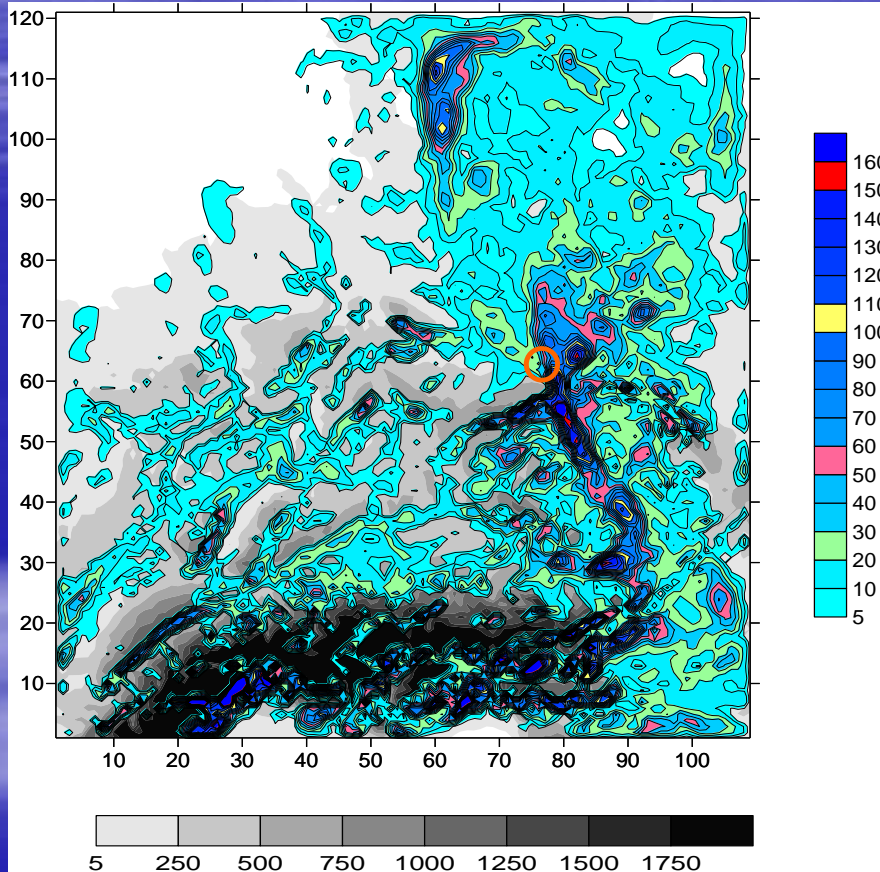


# Precipitation sum (mm) 12.08

07-18 h

Rate (48.8 mm)

REMO (47.0 mm)



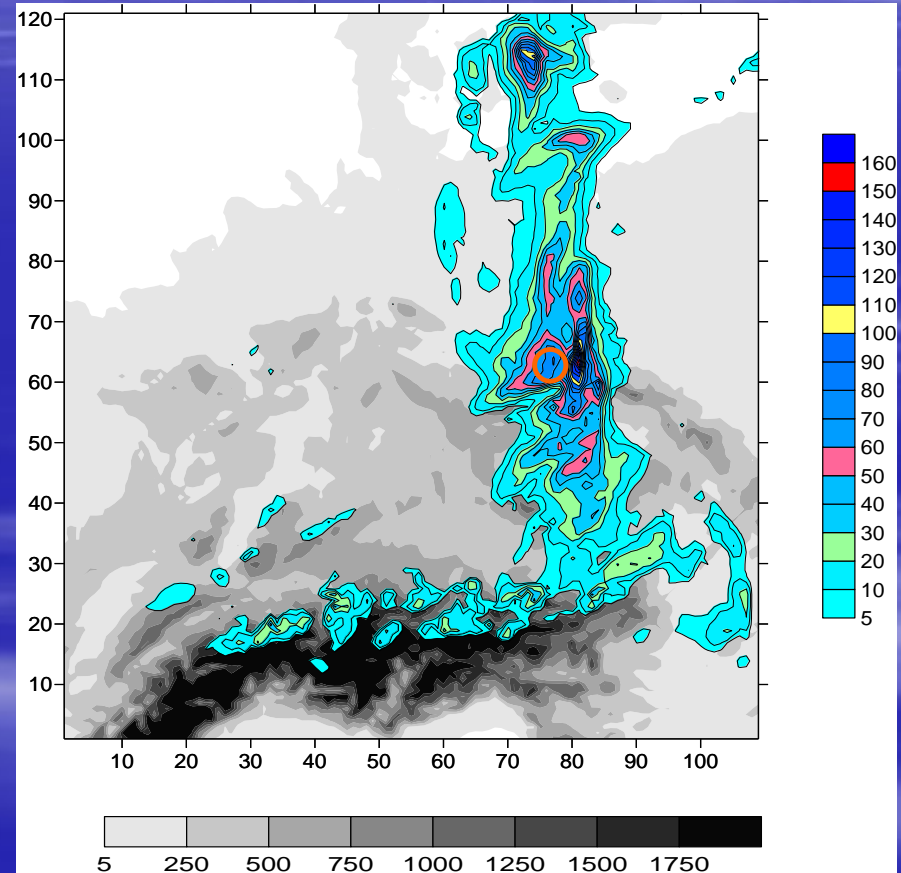
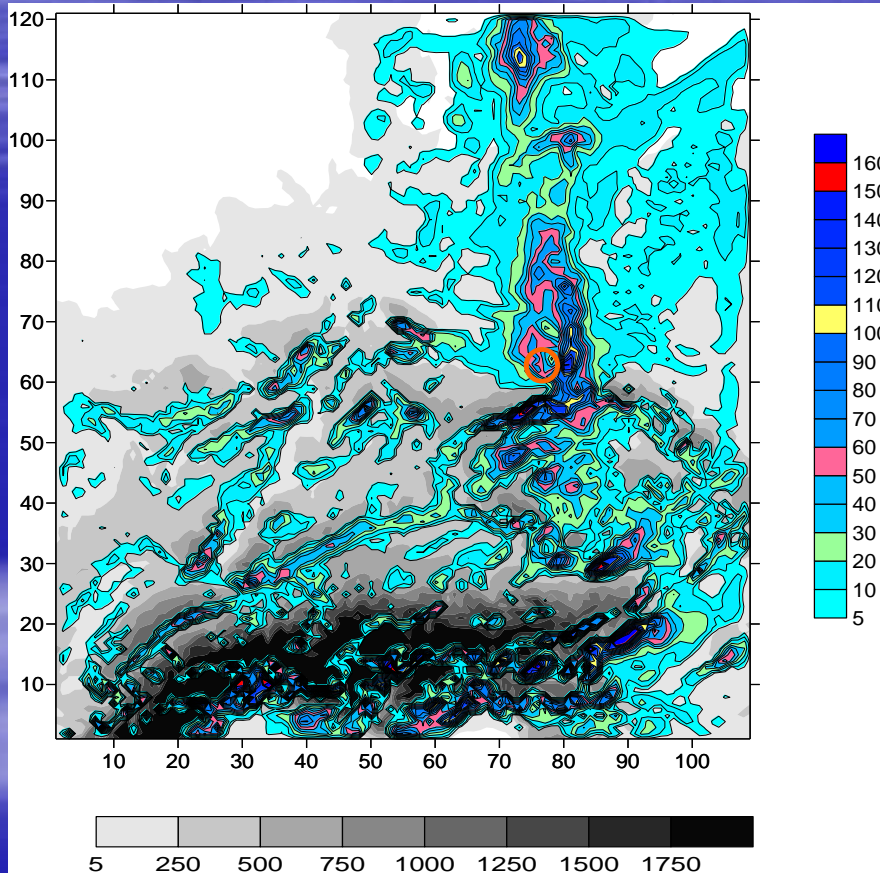
# Precipitation sum (mm)

12-13.08

19-06 h

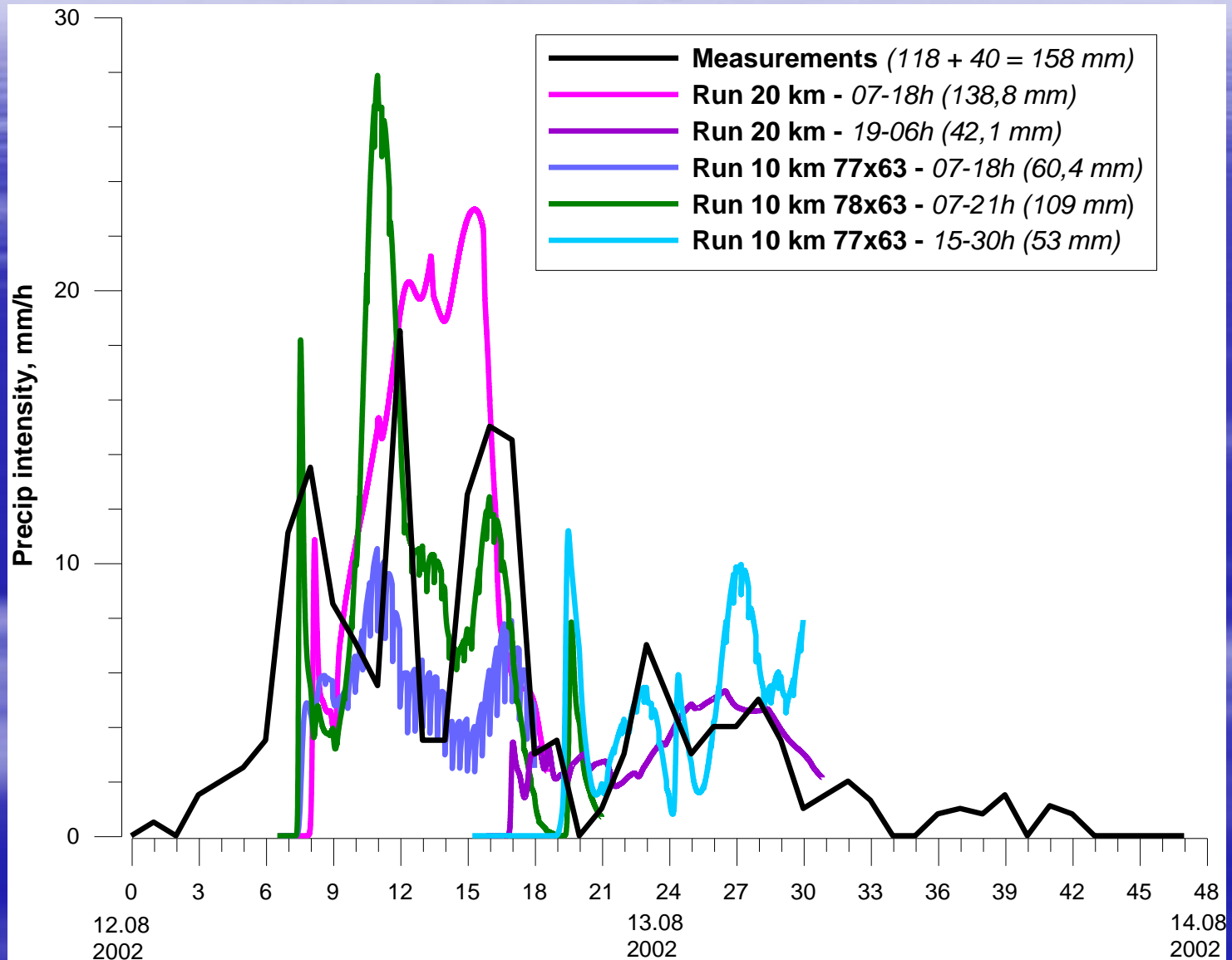
Rate (48.1 mm)

REMO (70.8 mm)





# Microphysical results (Dresden)

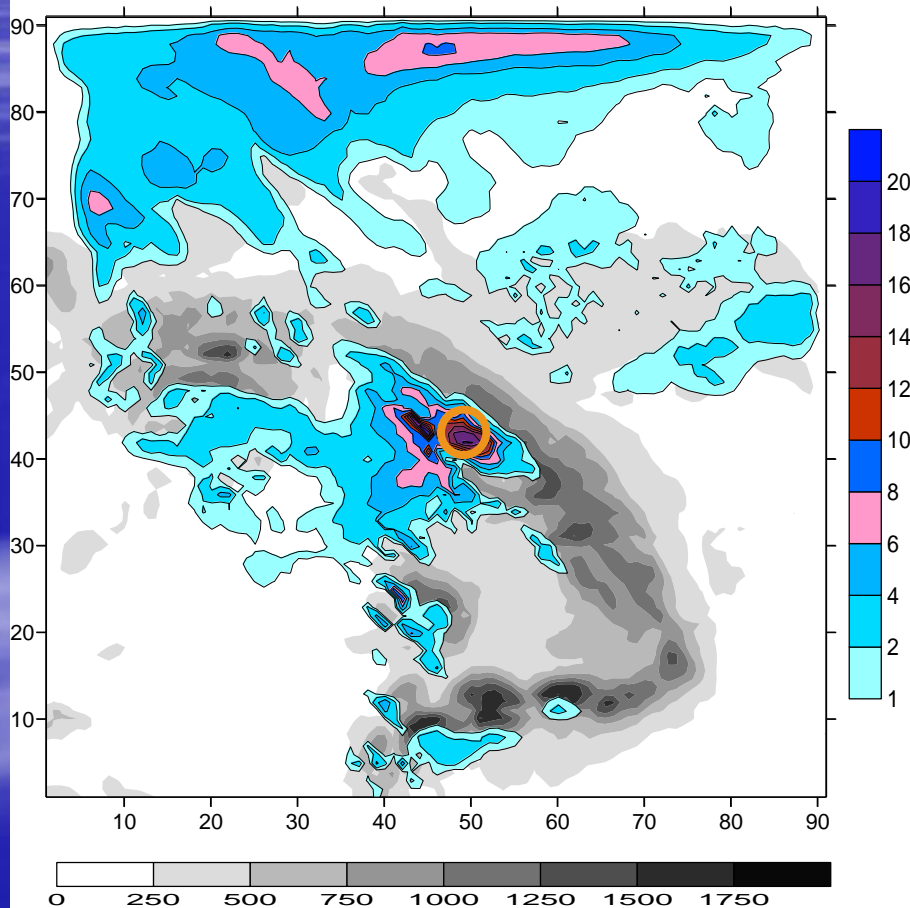


# Results of REMO and CMCT (Carpathians)

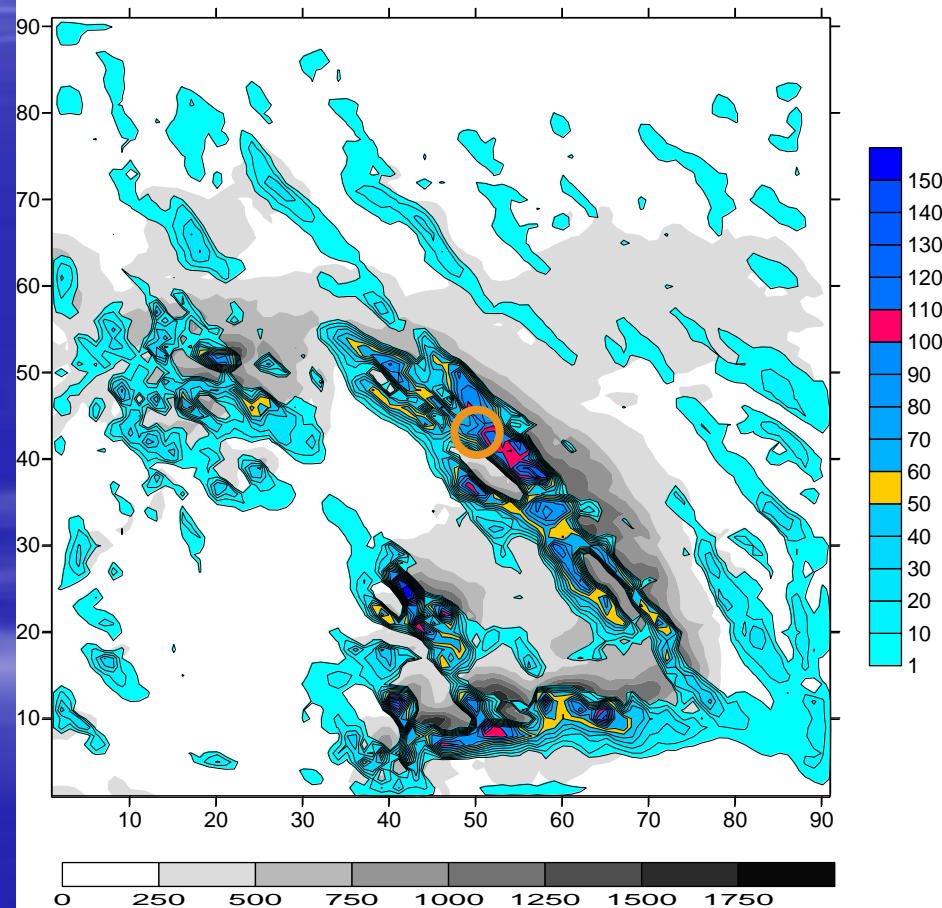
**Measured:** Mizhirja = 10,6 mm; Ust-Chorna = 5,2 mm

**REMO** – good; **rate** indicates further intensification up to 50 mm

REMO precipitation (mm)  
Sum 07-18h 3.11.1998

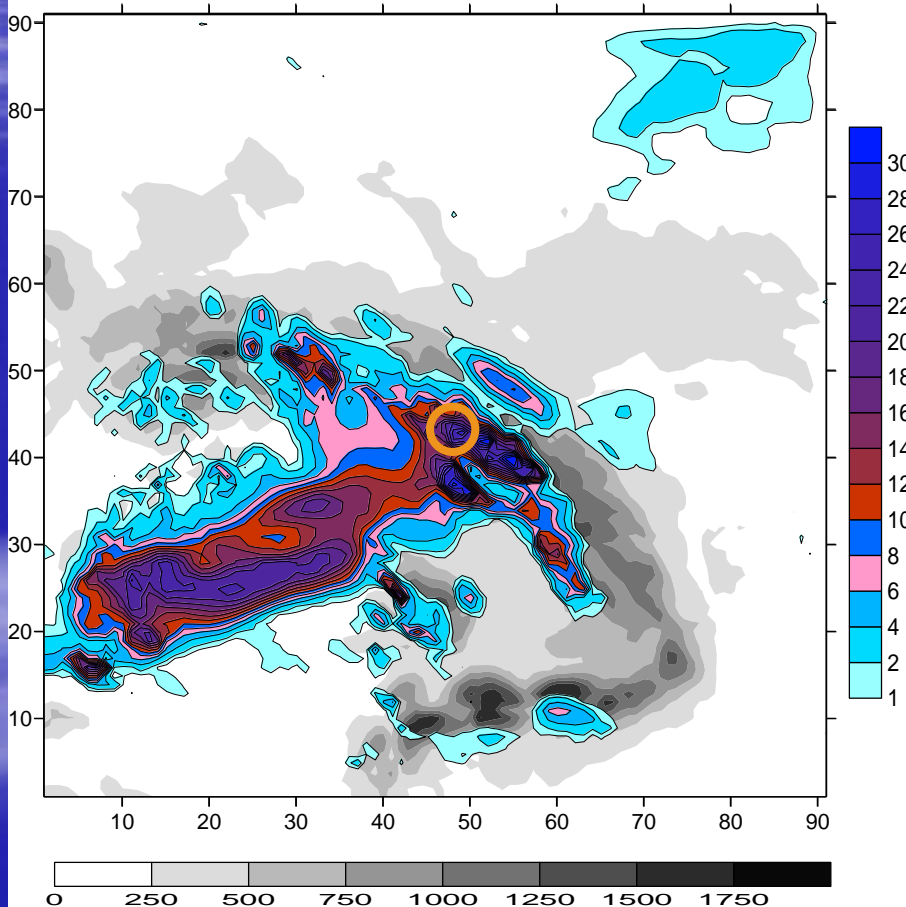


Integral thermodynamic condensation rate (mm)  
Sum 07-18h 3.11.1998

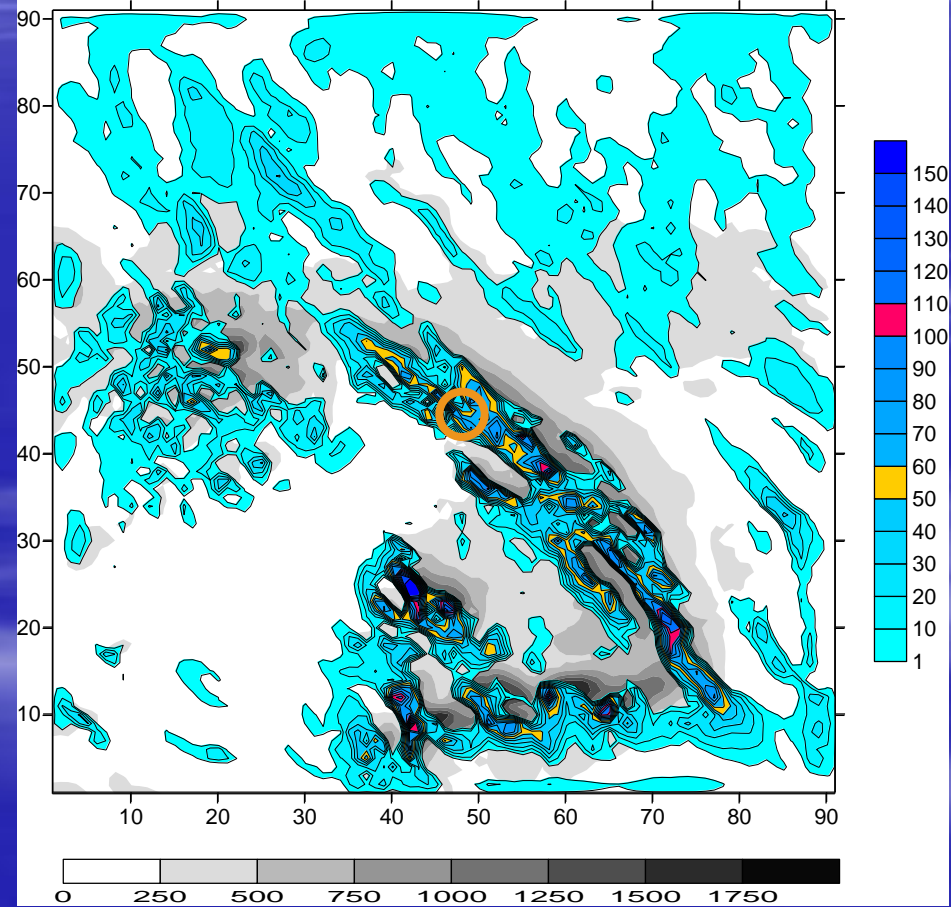


**Measured:** Mizhirja = 32,9 mm; Ust-Chorna = 64,2 mm  
**REMO** – less (15-30 mm); **rate** – 40-70 mm and indicates that precipitation intensity will be the same in the next period

**REMO precipitation (mm)**  
Sum 19 - 06h 3.11.1998



**Integral thermodynamic condensation rate (mm)**  
Sum 19-06h 3.11.1998

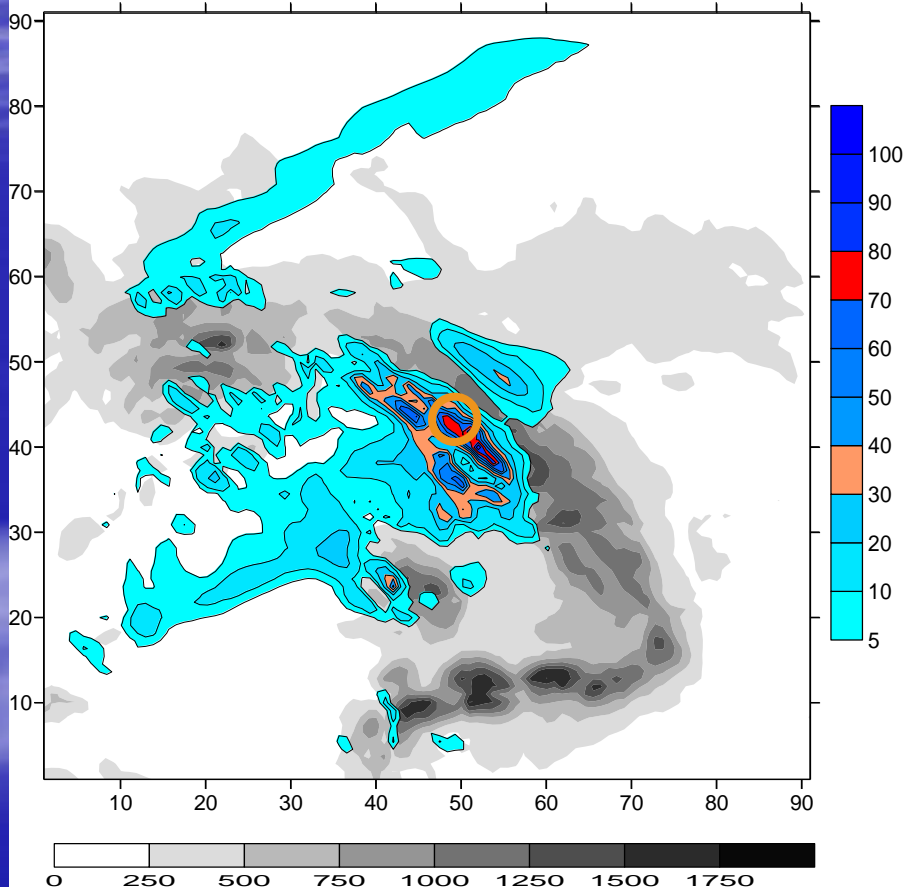




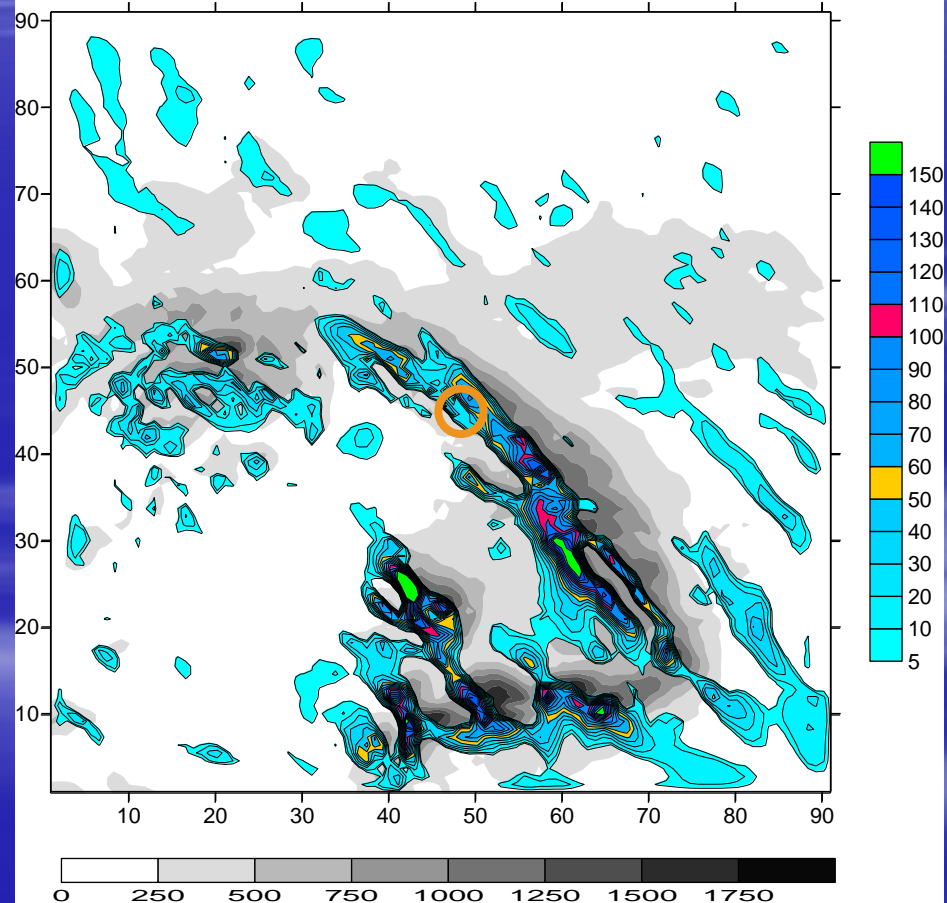
**Measured:** Mizhirja = 80,2 mm; Ust-Chorna = 71,0 mm

**REMO** – good (*max 70 mm*); **rate** – 30-80 mm and indicates that precipitation intensity will be a bit less in the next period

**REMO precipitation (mm)**  
Sum 07 - 18h 4.11.1998

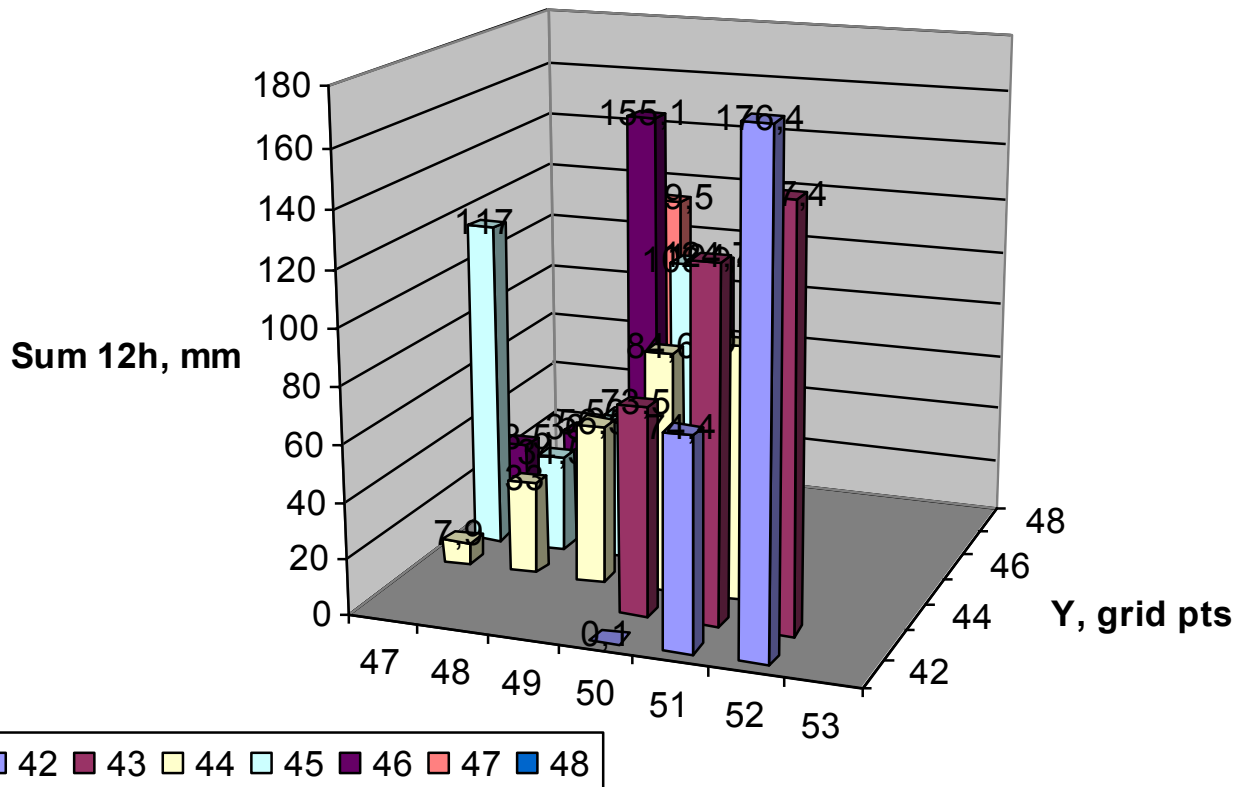


**Integral thermodynamic condensation rate (mm)**  
Sum 07-18h 4.11.1998



# 12h precipitation sum from two microphysical runs started at 06h and 12h 04.11.1998

X x Y	47	48	49	50	51	52
47			119,5			
46	28,5	36,5	<b>155,1</b>	104,4		
45	<b>117</b>	<b>34,5</b>	52,4	109,9		
44	<b>7,9</b>	<b>33</b>	56,5	84,6	90,3	
43				<b>73,5</b>	<b>124,7</b>	<b>147,4</b>
42				<b>0,1</b>	<b>74,4</b>	<b>176,4</b>



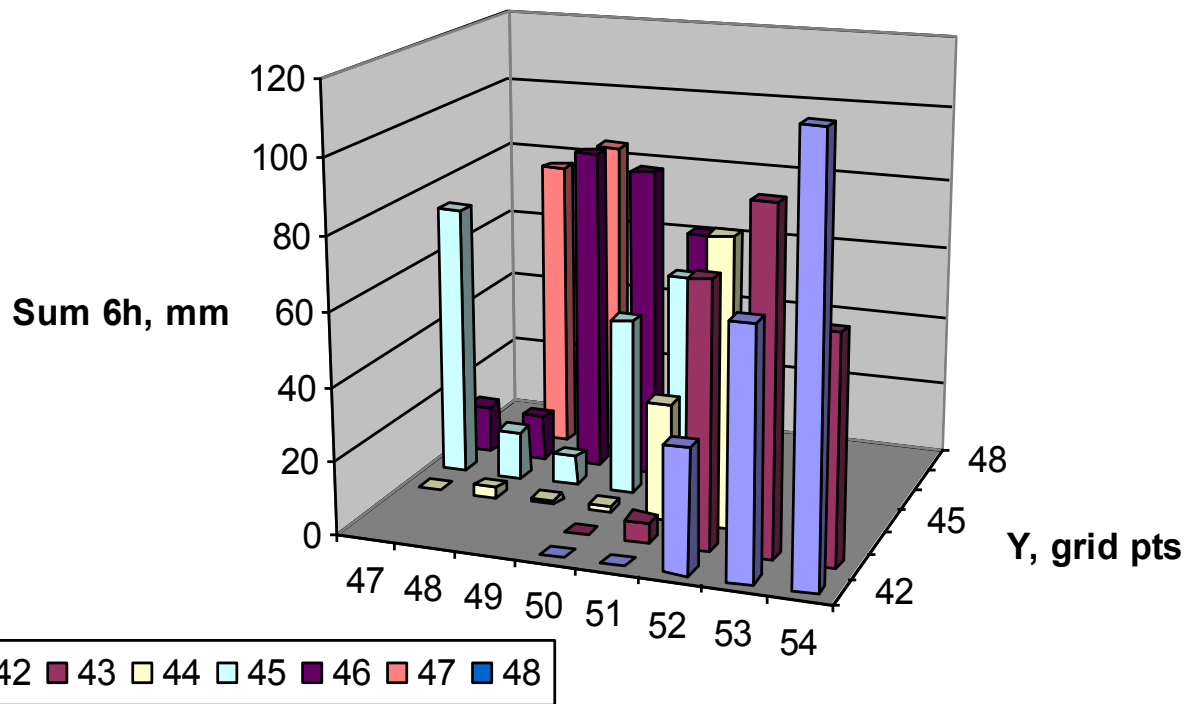
Mizhirja  
47.3 x 44.4 pts  
Gauge 80,2 mm

Ust-Chorna  
50.4 x 42.4 pts  
Gauge 71,0 mm

Aver. 20 gridboxes  
81,3 mm  
Snow - 10-30%

6h precipitation  
sum from the  
microphysical run  
started at 18h  
04.11.1998

X x Y	47	48	49	50	51	52
47		80,7	88			
46	13,4	12,3	<b>89,5</b>	85,7	69,6	
45	<b>74,8</b>	<b>12,9</b>	8,1	48,3	62	
44	<b>0</b>	<b>2,7</b>	1,4	1,9	32	<b>78,6</b>
43				0	5,6	71,9
42				0	0	33,7



Mizhirja  
47.3 x 44.4 pts  
70,0 mm (12h)

Ust-Chorna  
50.4 x 42.4 pts  
66,1 mm (12h)

Aver. 30 gridboxes  
44,1 mm (6h)  
Snow - up to 60%



# Conclusions

- Rates of condensation obtained in CMCT were close to maxima of precipitation intensities and indicated on cloud systems potentiality to produce heavy precipitation within next 3 - 6 hours.
- The spectral microphysical 1D model represented timing of precipitation development reasonably good
- The runs with spectral microphysics revealed the importance of cold processes in the clouds in particular for the colder cases in the Carpathians.
- All models still have problems with simulation heavy precipitation in mountainous regions due to complicated dynamical processes there.

**ДЯКУЮ!**

**THANK YOU !**

**DZIĘKUJĘ !**

Ukrainian Antarctic station "Akademik Vernadsky" through an iceberg window

*(Foto by Krakovska S. 1998)*