

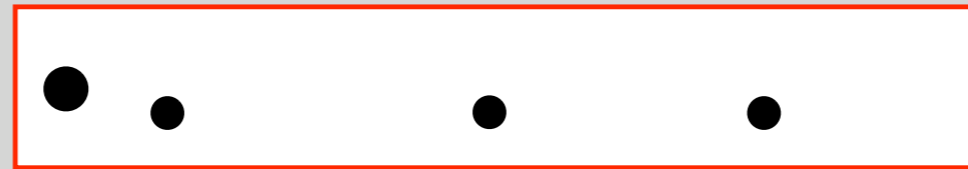
EMPM vs DNS results of Kumar, Schumacher, and Shaw (2014)

For same number of droplets (~ 9 million) and duration (30 minutes) as the DNS, the EMPM requires only 5 cpu hours.

EMPM diagram

EMPM with droplets and entrainment

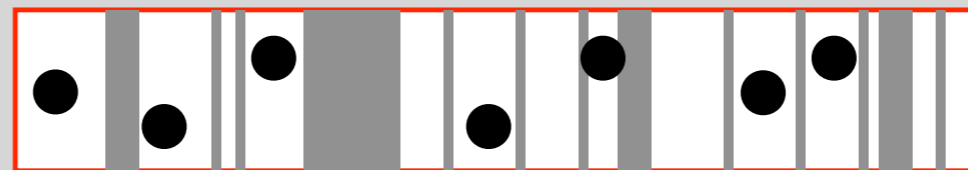
← 100 m →



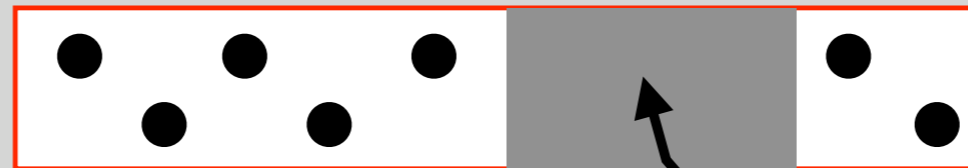
droplet evaporation



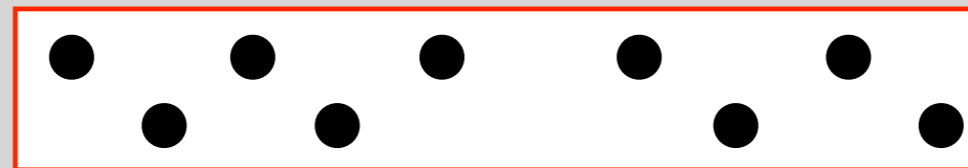
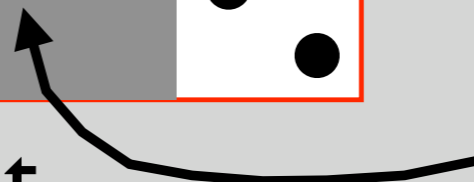
molecular diffusion



turbulent deformation



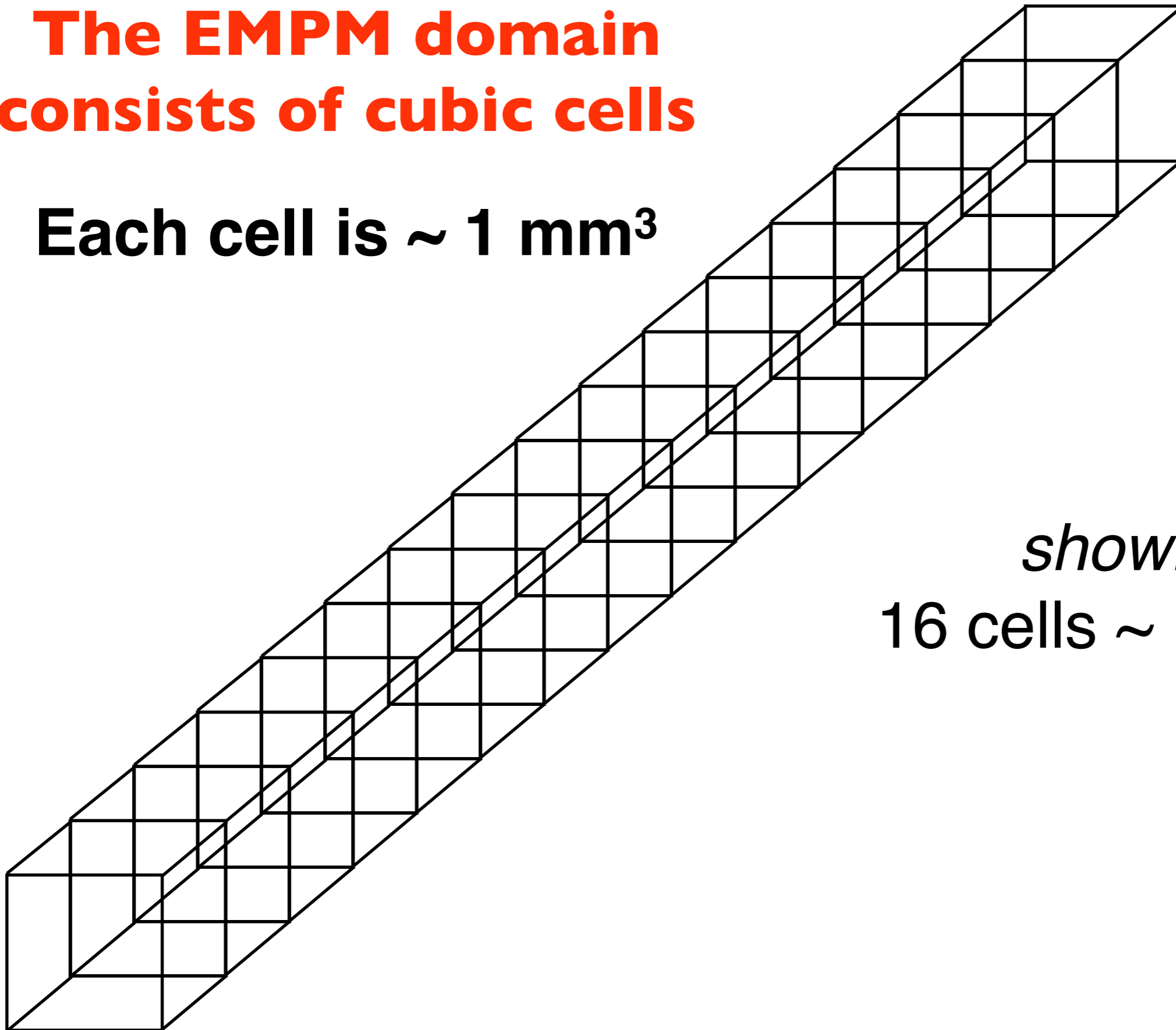
entrainment



saturated parcel

**The EMPM domain
consists of cubic cells**

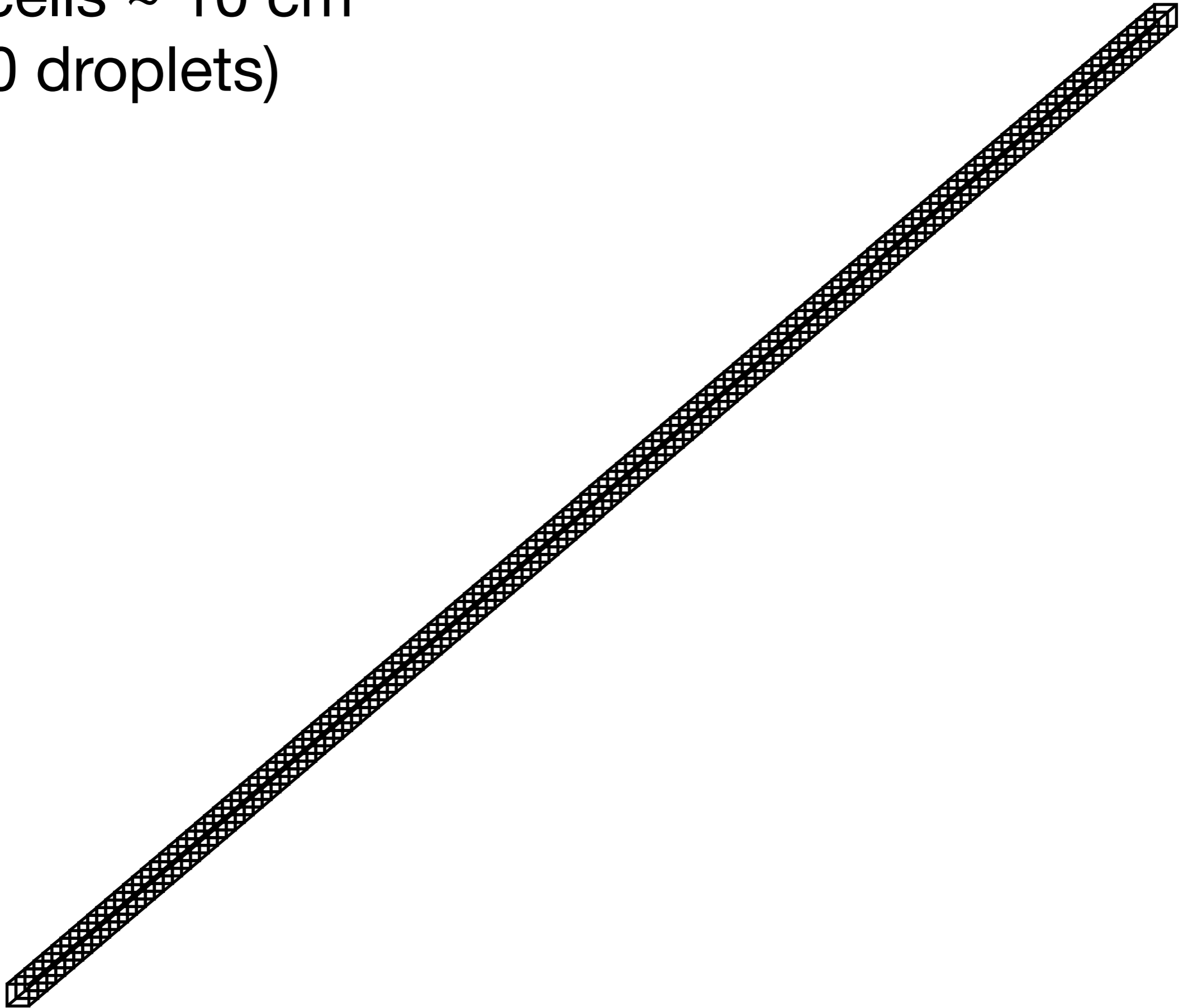
Each cell is $\sim 1 \text{ mm}^3$



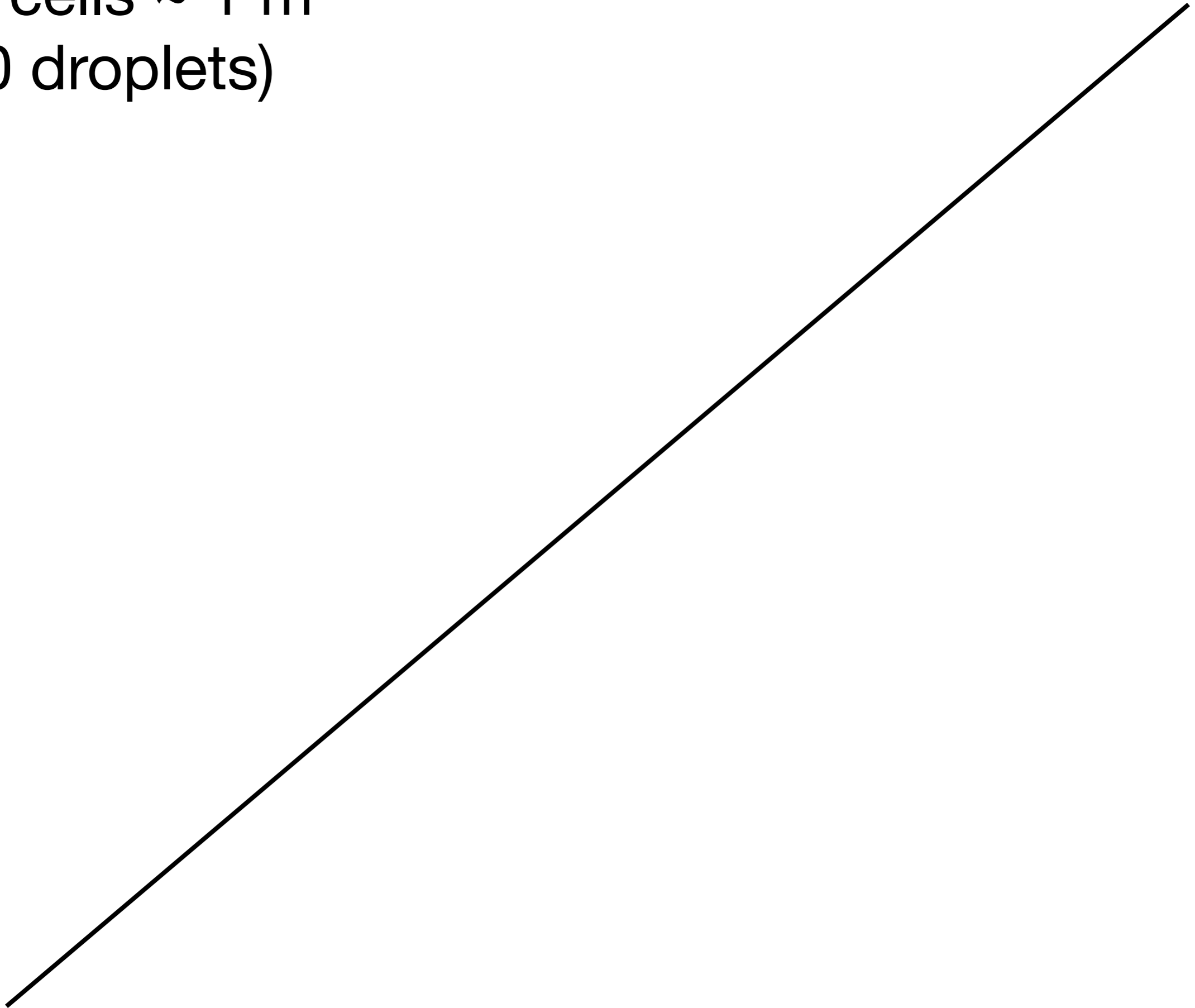
shown:

16 cells $\sim 1.6 \text{ cm}$

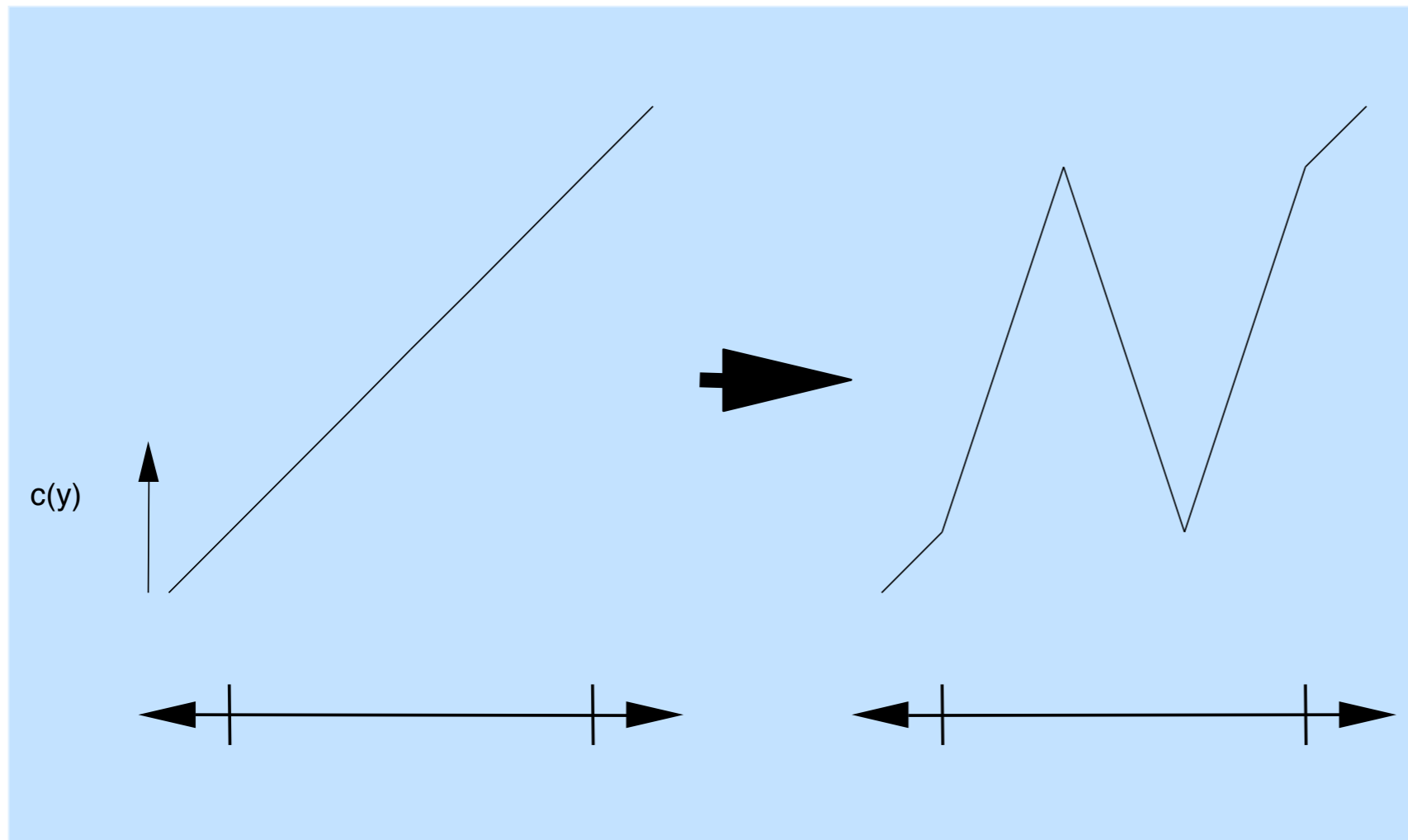
128 cells ~ 10 cm
(10 droplets)



1024 cells ~ 1 m
(100 droplets)



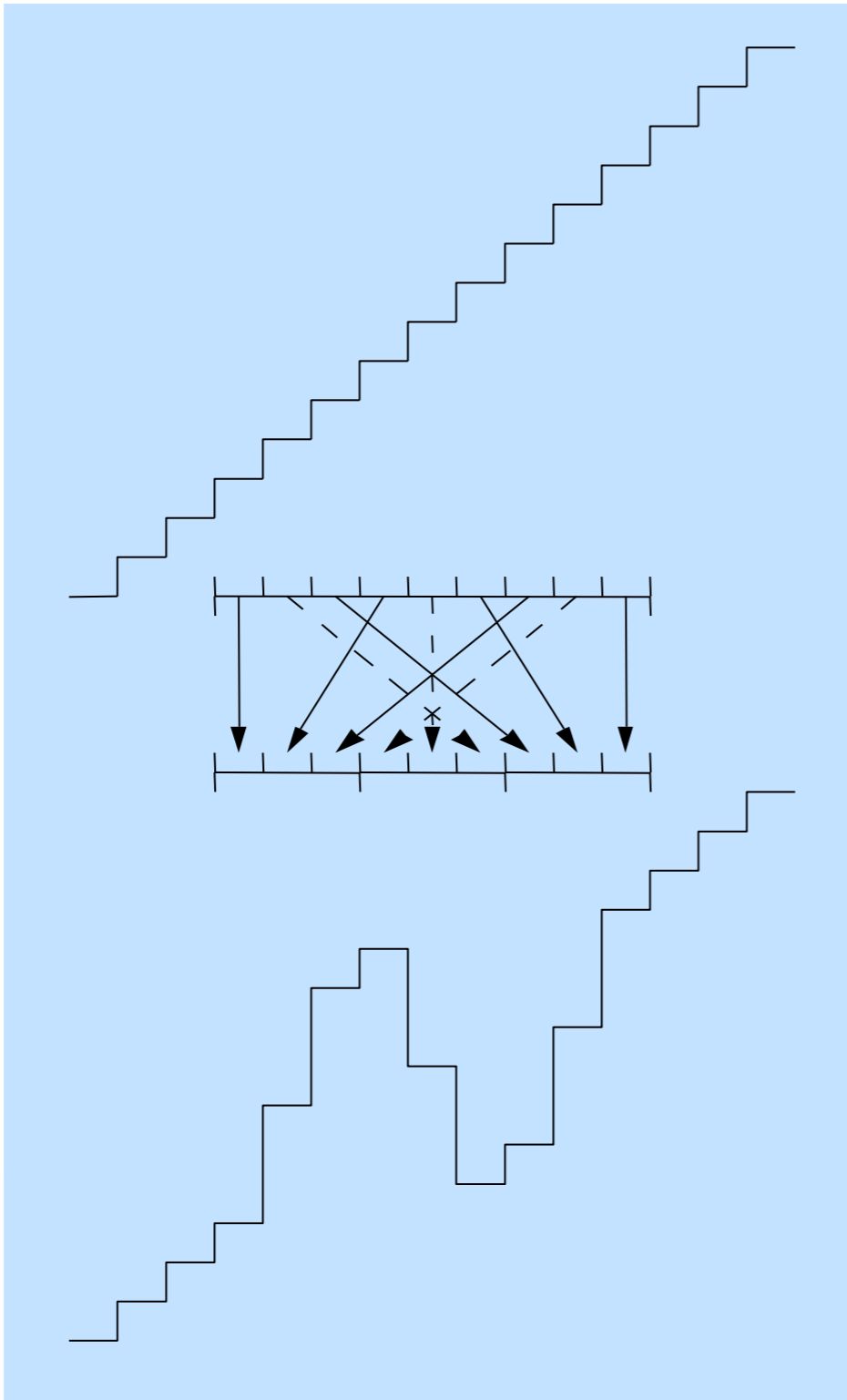
Turbulent motion of *fluid elements* is modeled as a sequence of **triplet maps** that preserve desired advection properties, even in 1D



The triplet map captures compressive strain and rotational folding effects, and causes no property discontinuities.

Alan Kerstein

Turbulent motion of *fluid elements* is modeled as a sequence of **triplet maps** that preserve desired advection properties, even in 1D



The triplet map is implemented numerically as a permutation of fluid cells.

Triplet Map for Fluid Elements

Each triplet map has a location, size, and time.

- *Location* is randomly chosen.
- *Size* l is randomly chosen from a distribution that matches inertial range scalings.
 - Smallest map (eddy) is Kolmogorov scale, η .
 - Largest eddy is L , usually domain size.
- Eddies occur at a *rate* determined by the large eddy time scale and eddy size range.

EMPM Fluid Variables

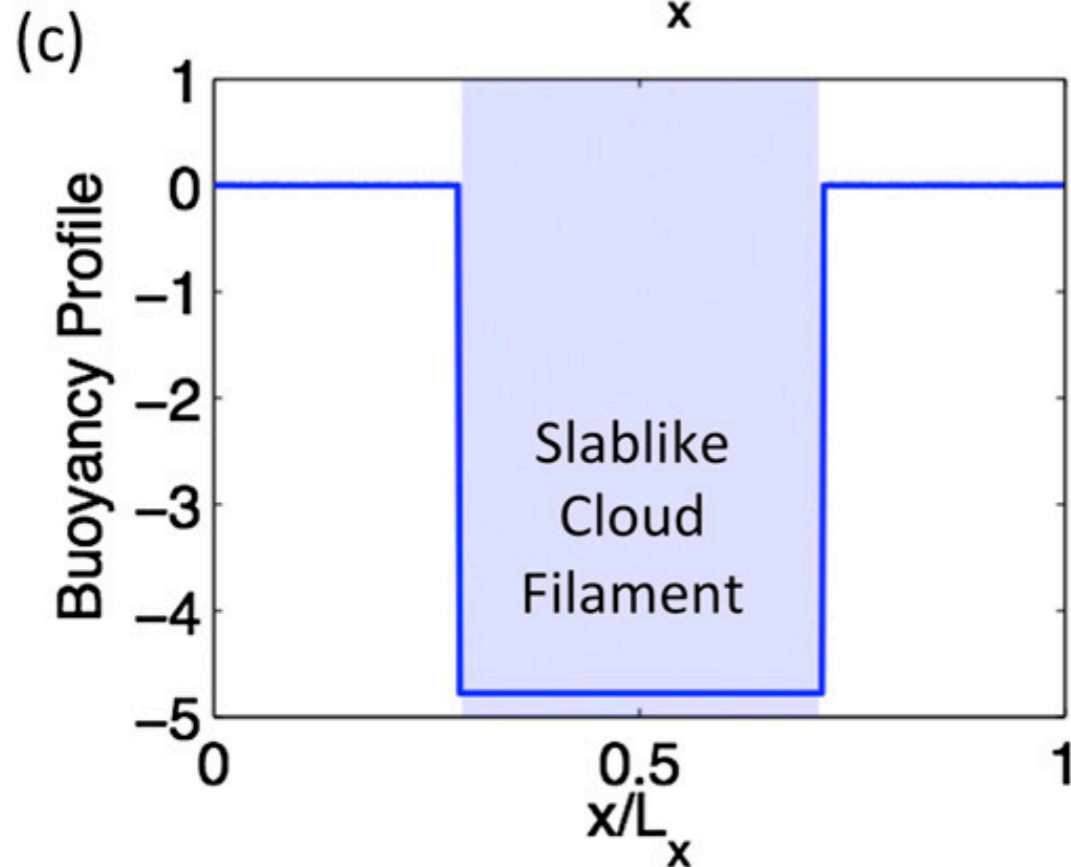
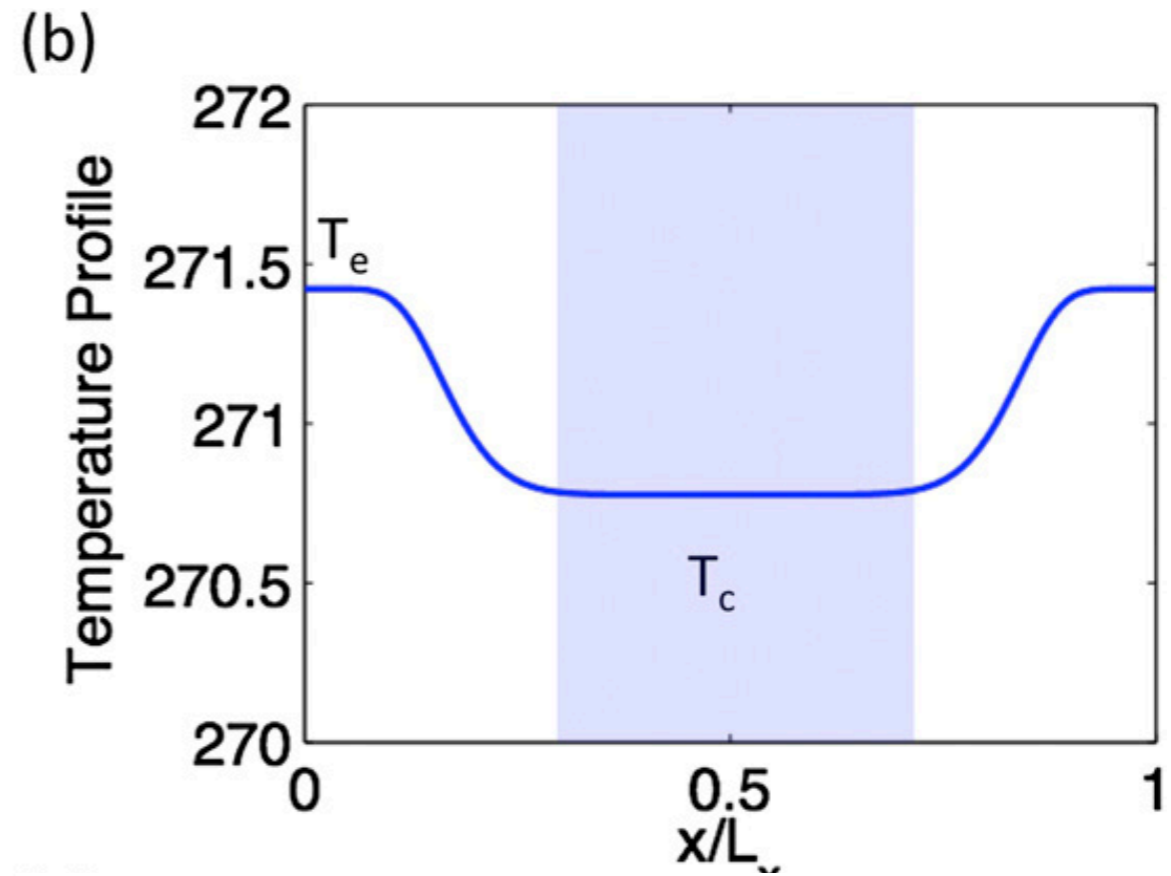
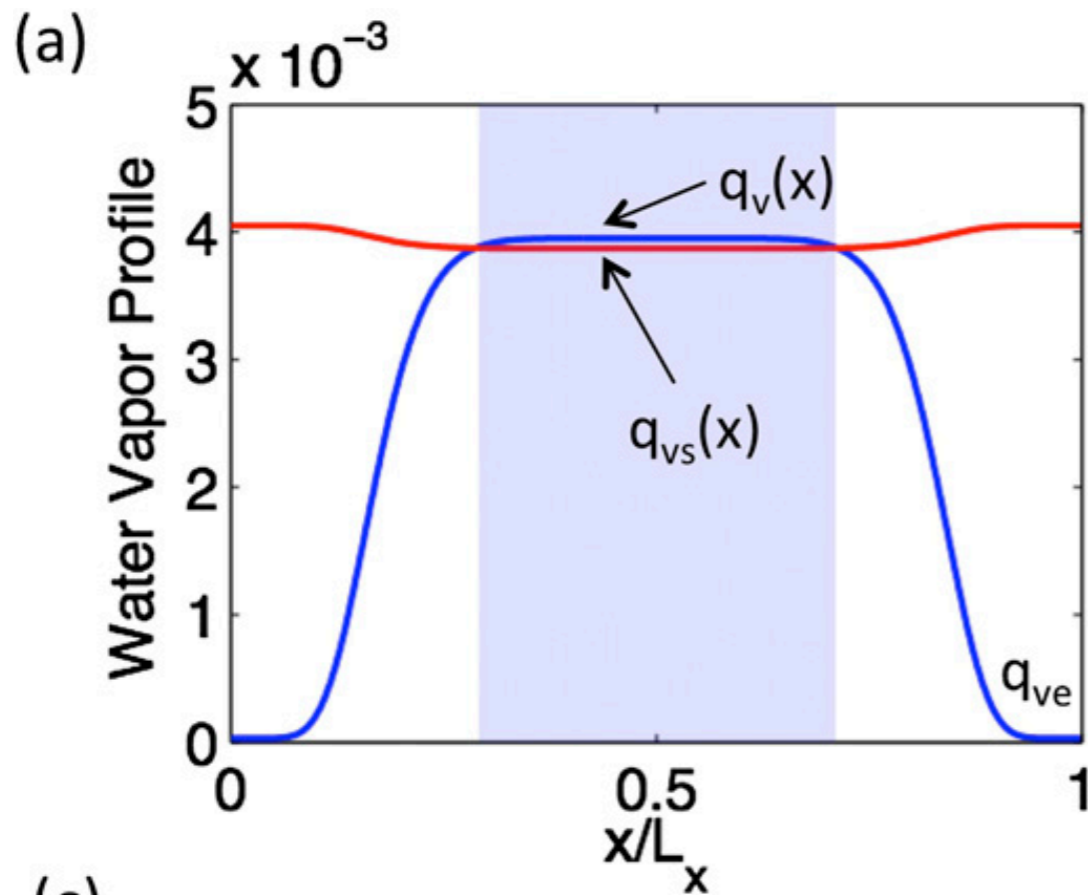
- Bulk microphysics:
 - Liquid water static energy
 - Total water mixing ratio
- Droplet microphysics:
 - Temperature
 - Water vapor mixing ratio

EMPM Droplet Variables

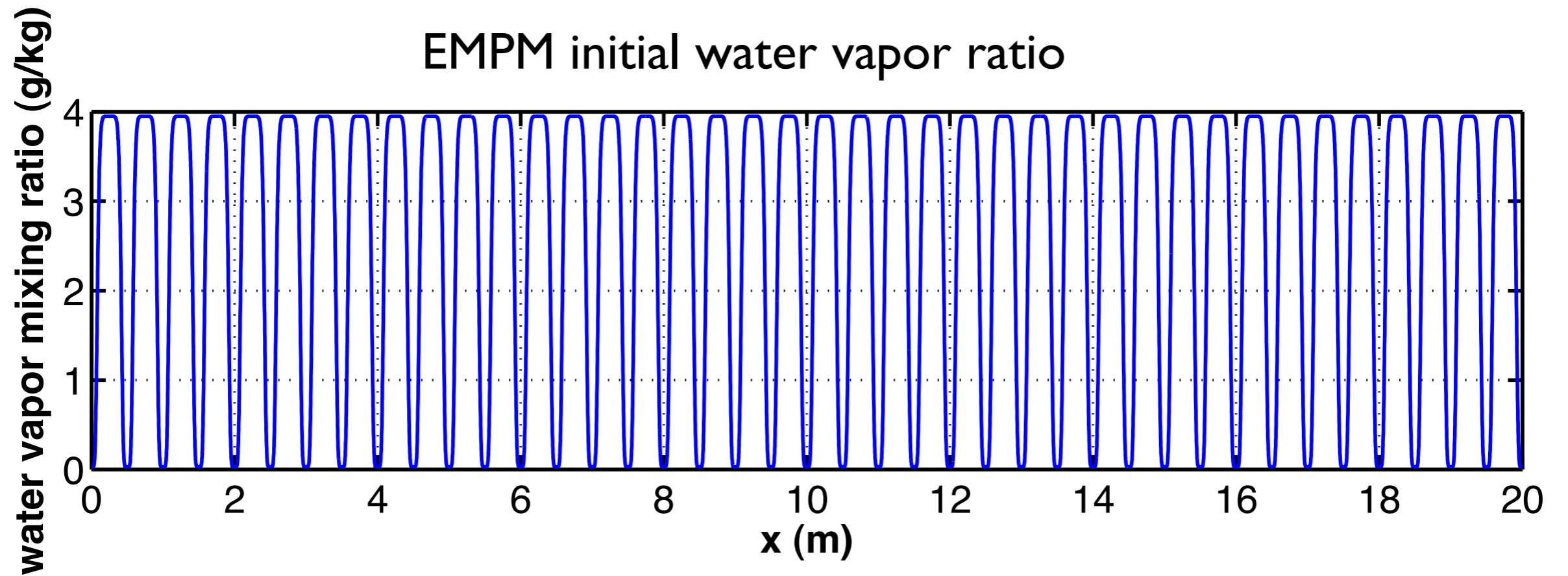
- **Location** (in one coordinate)
- **Radius** (droplet growth equation)
- CCN properties (specified)

In the EMPM, droplets move relative to the fluid at their terminal velocities.

Initial Configuration for DNS and EMPM



EMPM initial water vapor ratio



| | |
|----------------------|---------|
| Domain size | 20 m |
| Grid points | 12,000 |
| Grid size | 1.67 mm |
| Smallest 'eddy' size | 1 cm |
| Largest 'eddy' size | 0.5 m |
| Number of droplets | 1311 |
| Duration | 30 s |

1000 realizations (1.3M droplets) takes 45 CPU minutes.

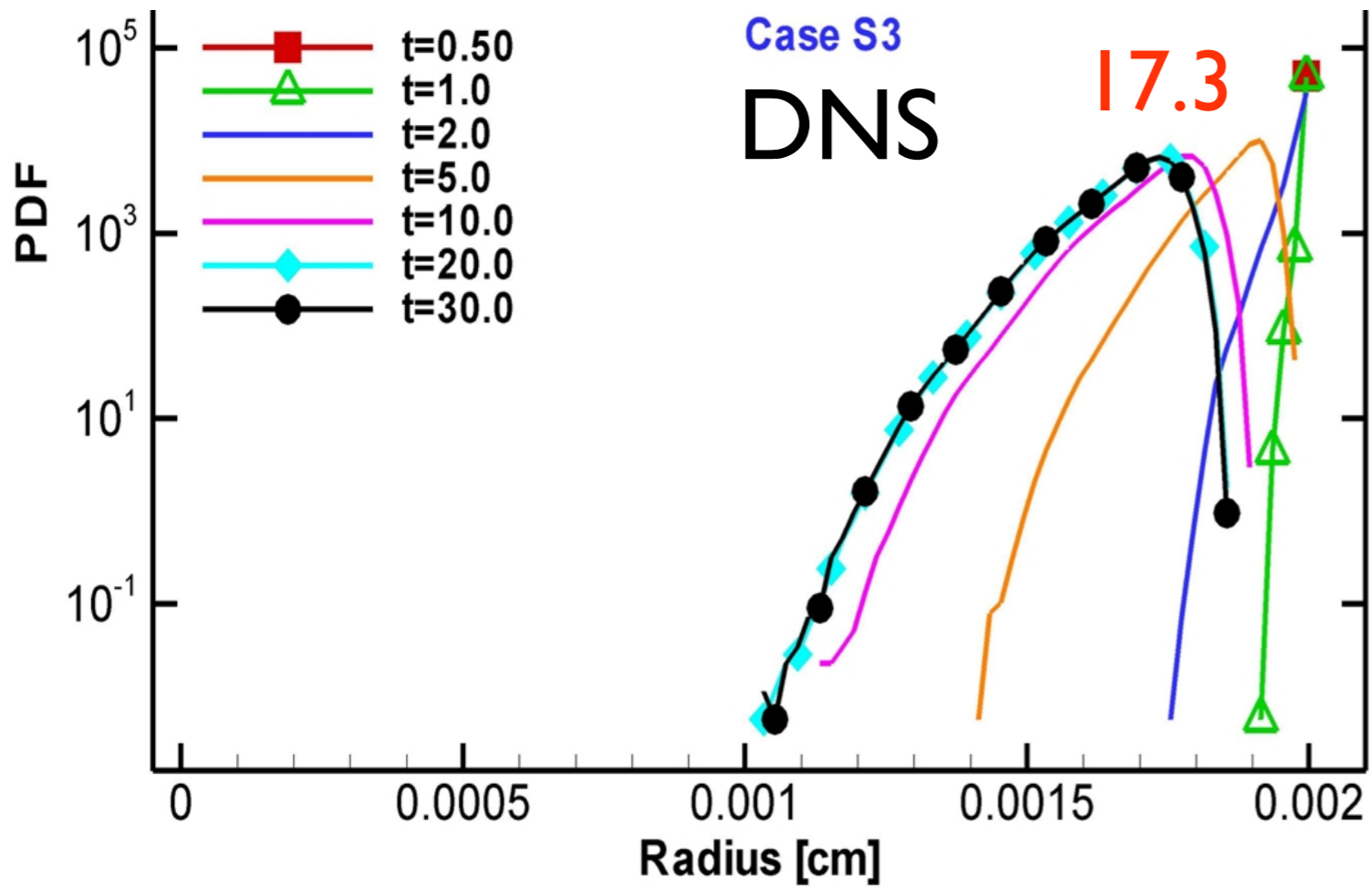
Some Potential Sources of Differences between the EMPM and DNS

- The EMPM's largest "eddy" (triplet map) size, L , should be set by matching the scalar variance decay time scale of the DNS.
- For these comparisons, L was simply set to the DNS domain size.
- In the EMPM, droplets fall parallel to the scalar gradients, thereby over-estimating the effects of droplet sedimentation.
- Not allowing droplets to fall underestimates sedimentation's impacts.
- We therefore performed simulations with and without sedimentation.

Some Potential Sources of Differences between the EMPM and DNS

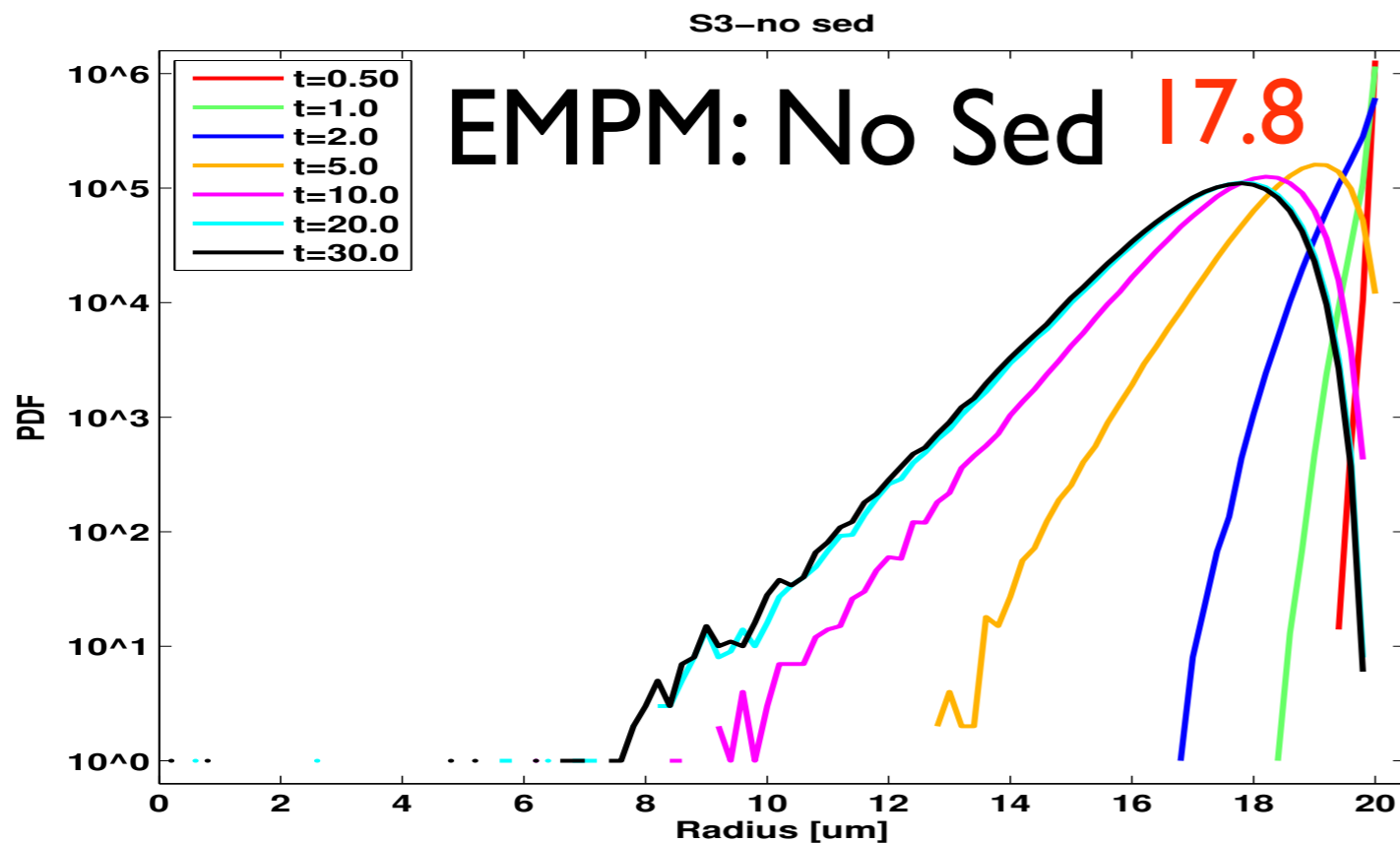
(Those listed below are not expected to be significant)

- The EMPM's turbulence properties are specified.
- They do not evolve in response to buoyancy due to droplet evaporation.
- Such buoyancy had a minor effect on mixing in the DNS.
- The EMPM's droplets have no inertia, unlike those in the DNS.
- The effects of droplet inertia on mixing should be much less than those of sedimentation.



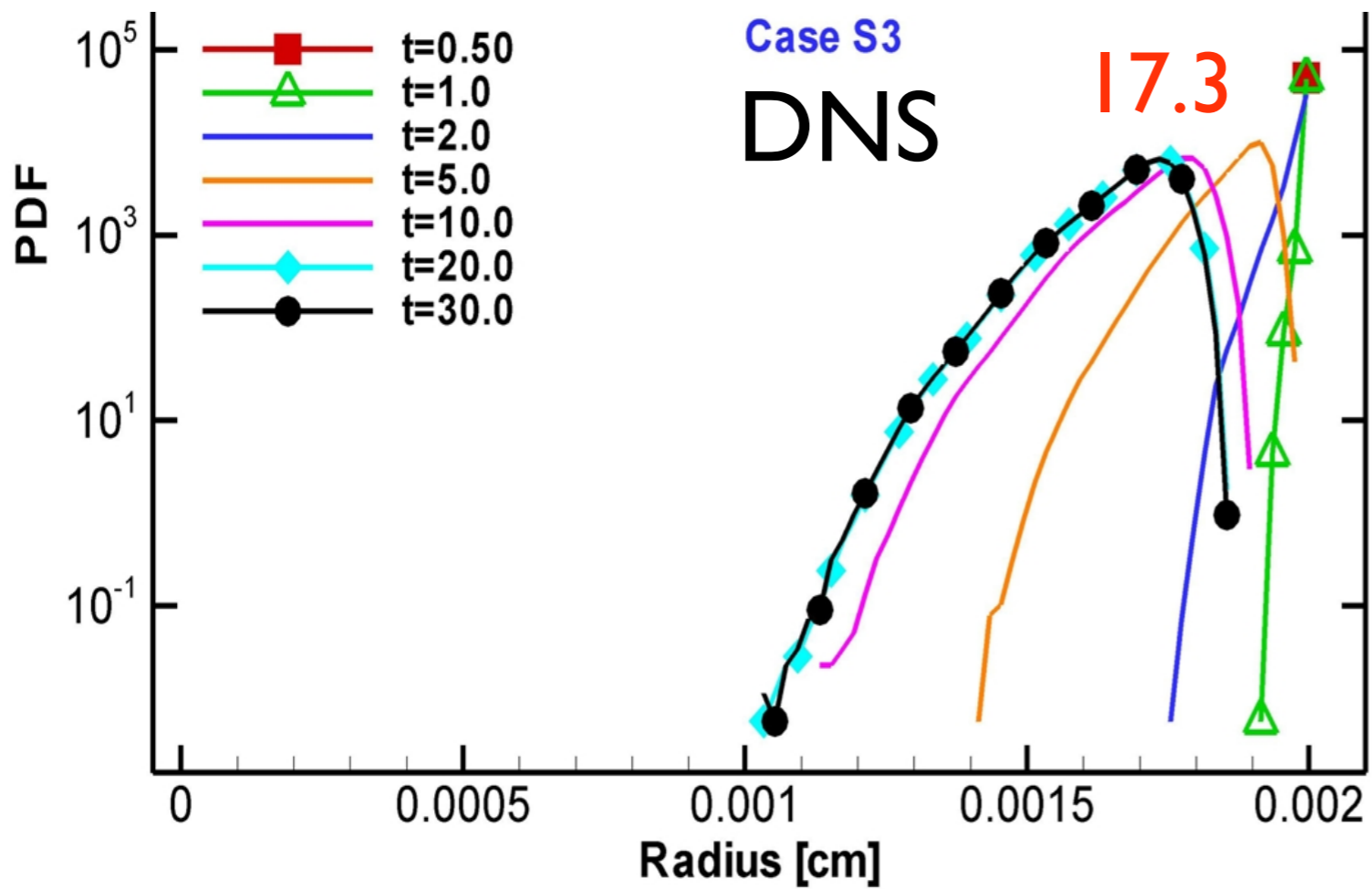
**Initial droplet
radius = 20 microns**

No droplets completely
evaporate.



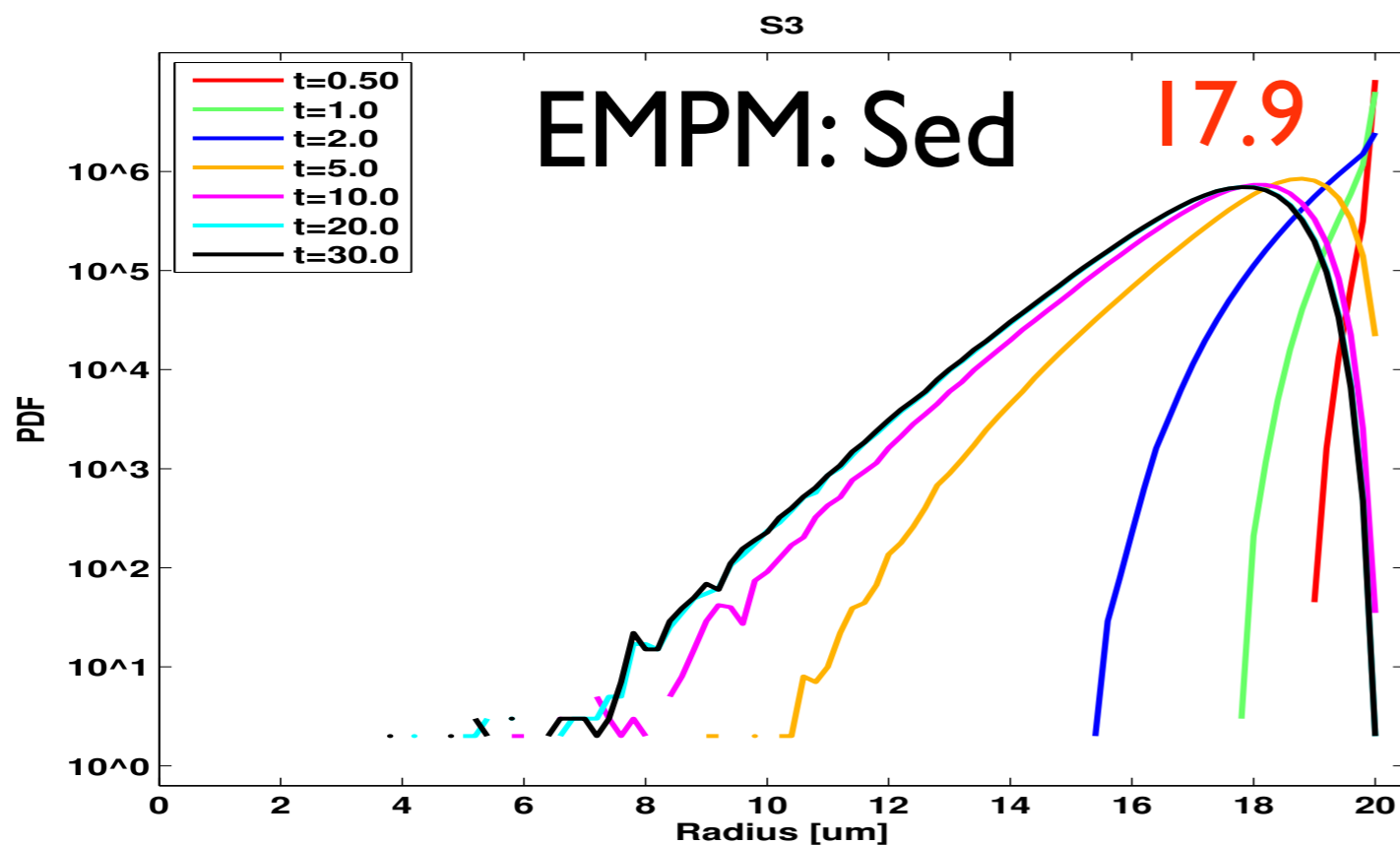
*DSD evolution is
essentially the
same.*

*Slightly wider DSD
at all times.*

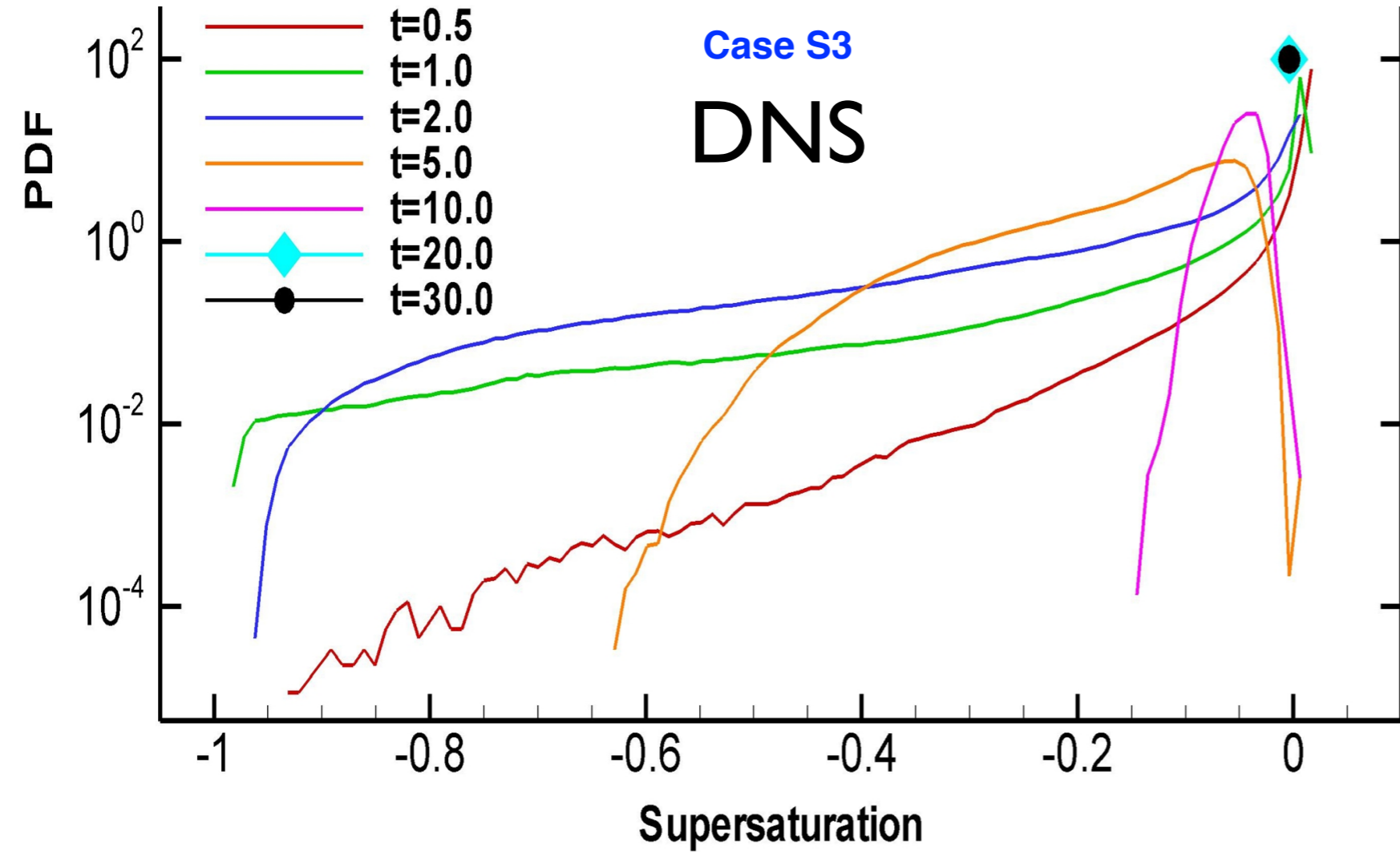


Initial droplet radius = 20 microns

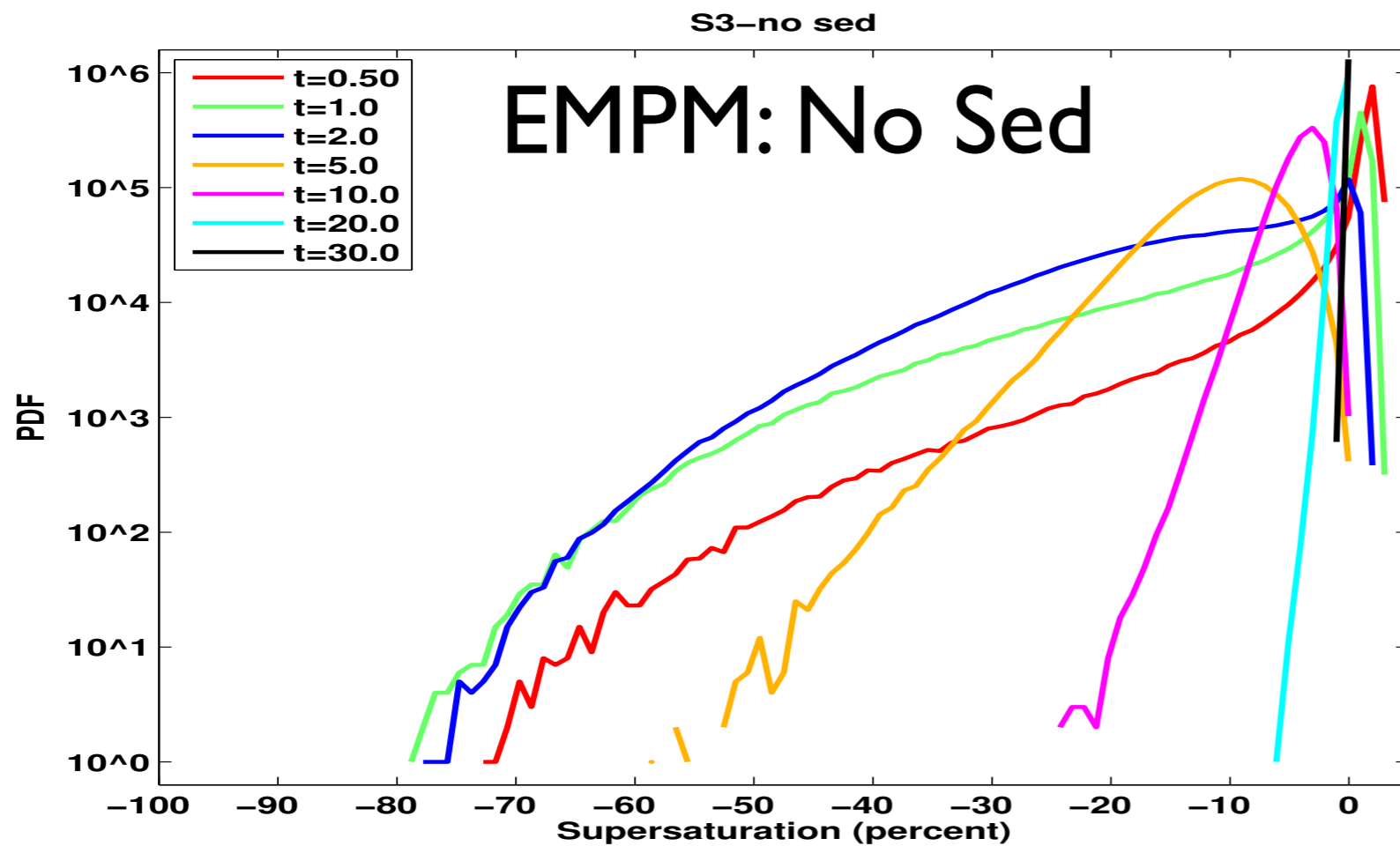
No droplets completely evaporate.



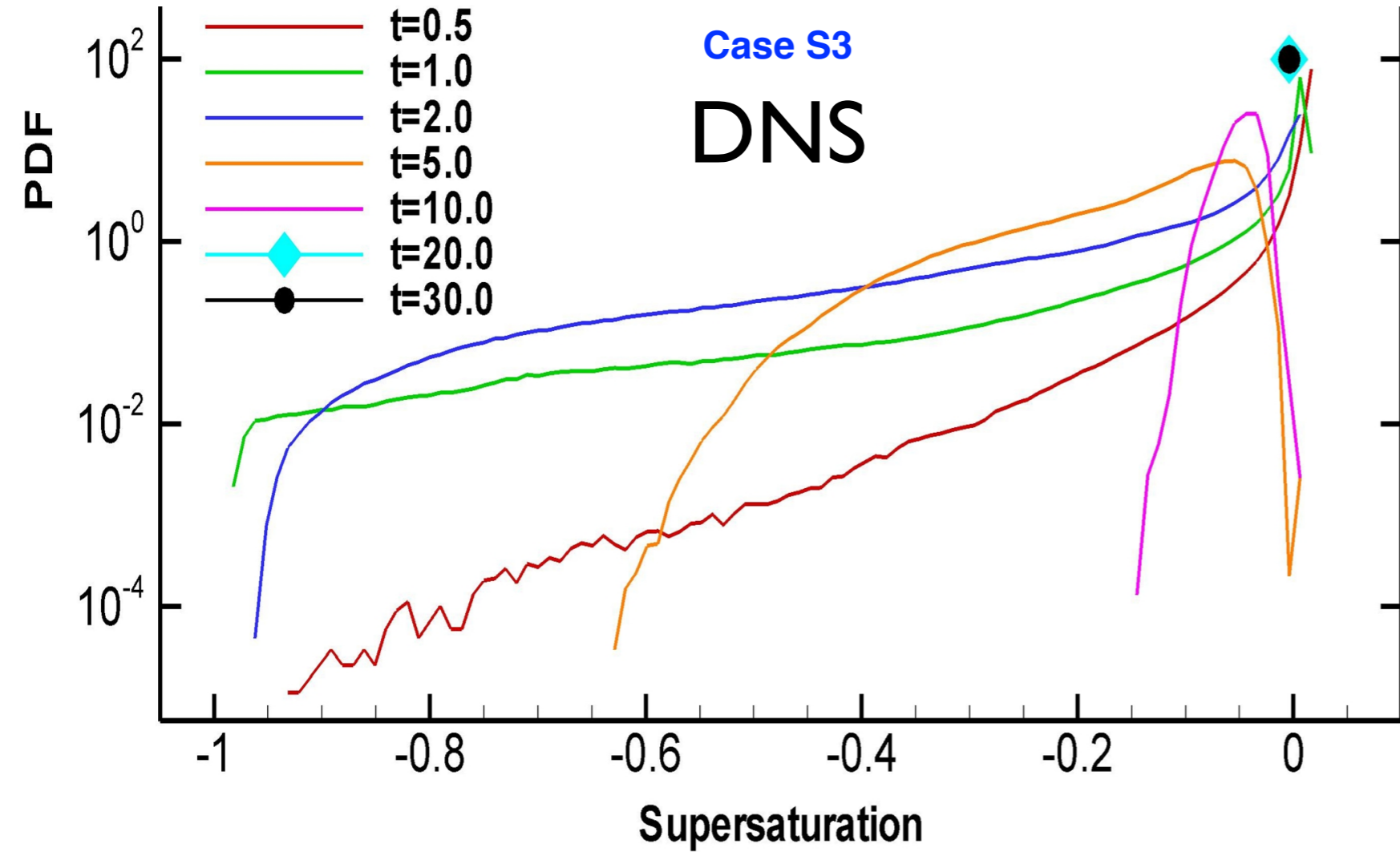
Slightly wider DSD than No Sed.



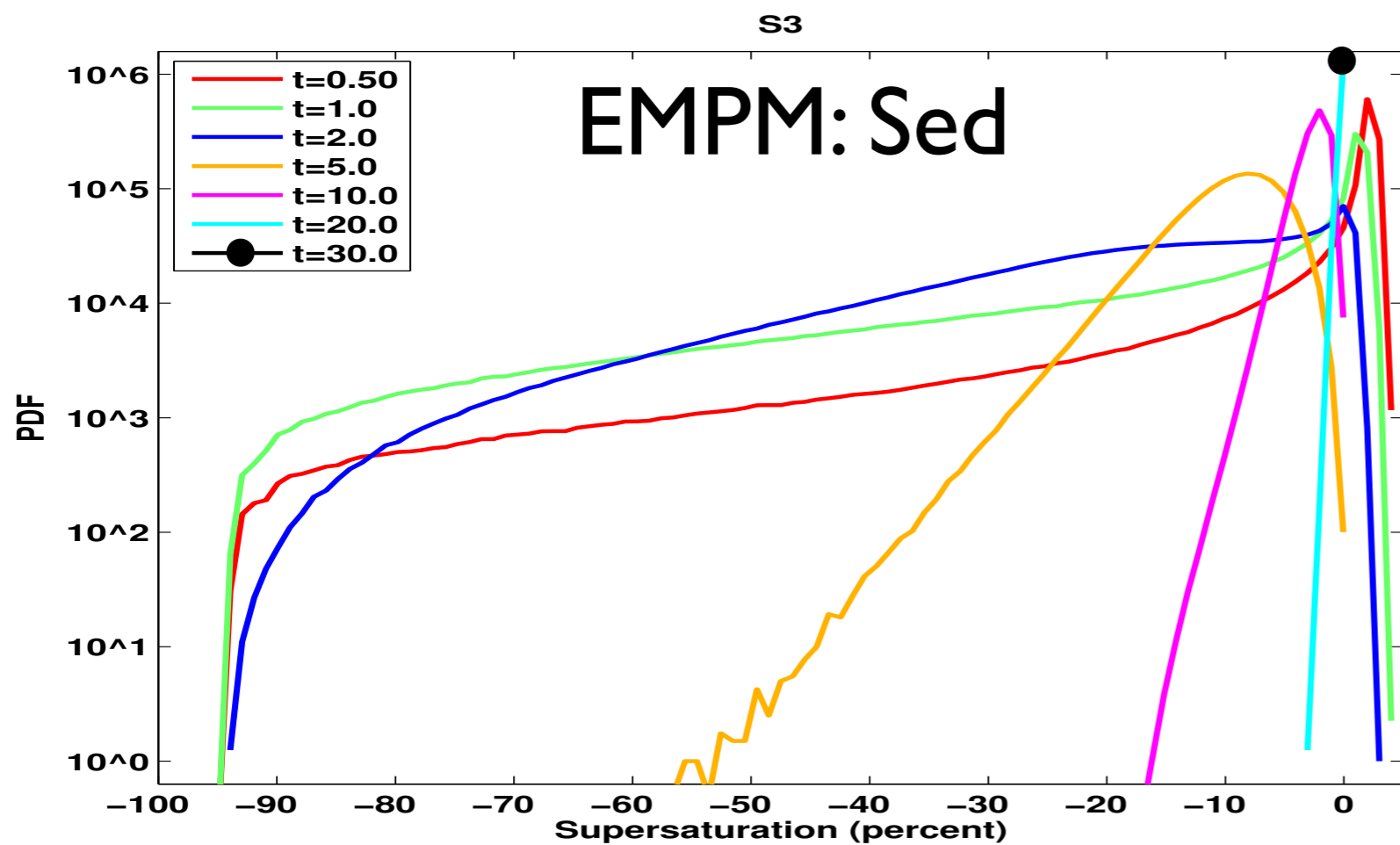
Super-saturation at droplets.



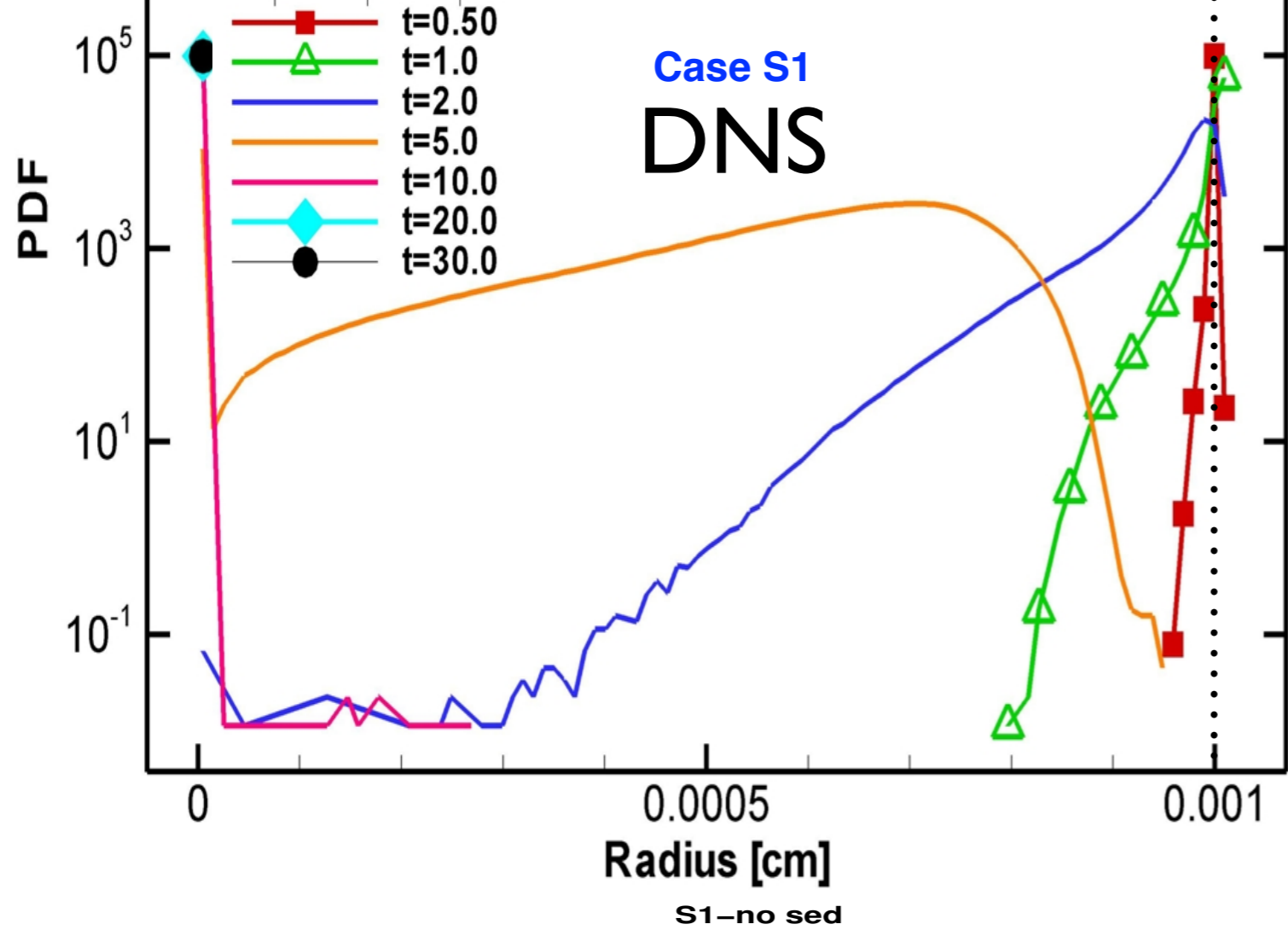
Droplets encounter less very dry air.



Super-saturation at droplets.



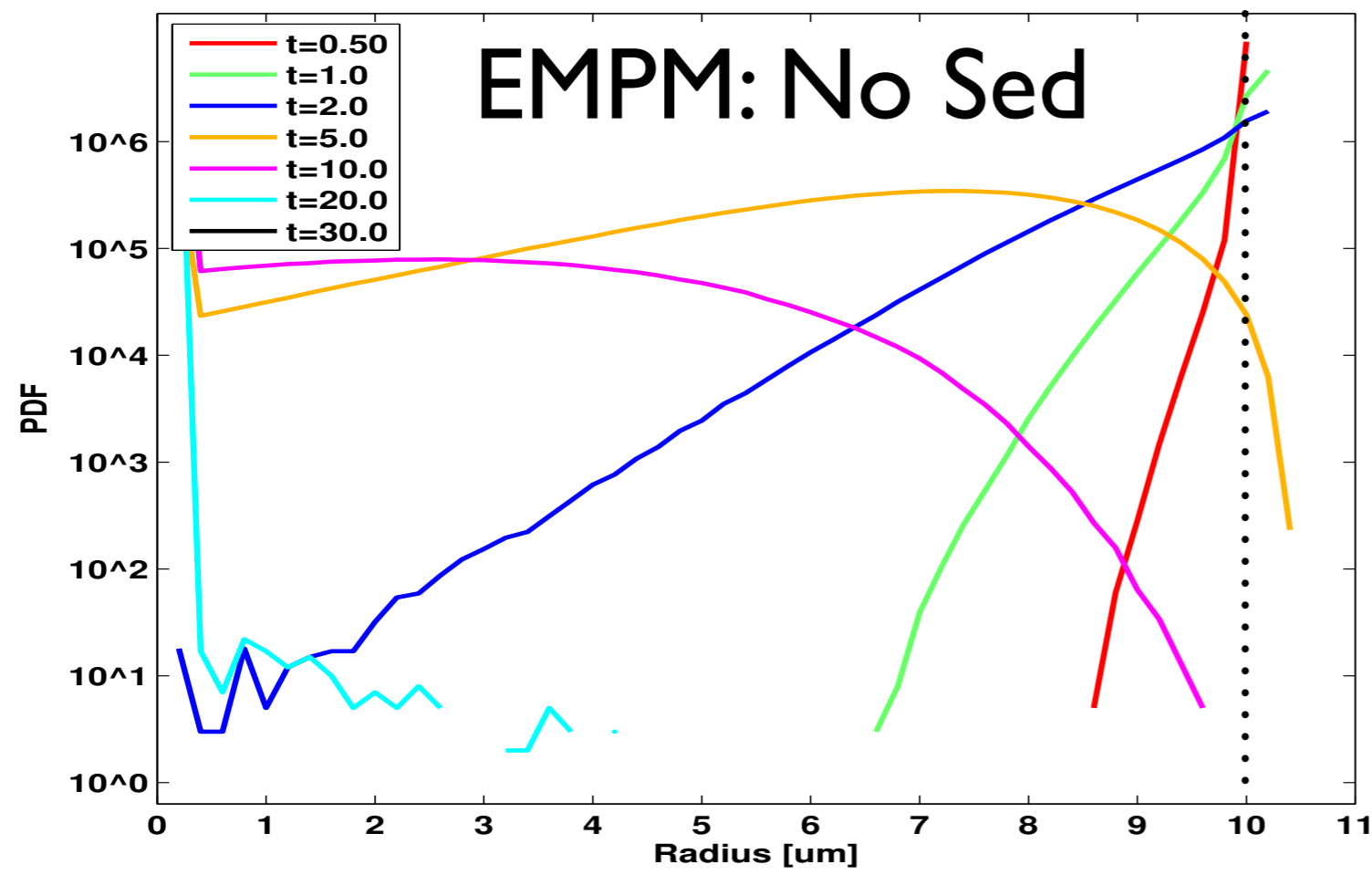
Droplets encounter more very dry air.



**Initial droplet
radius = 10 microns**

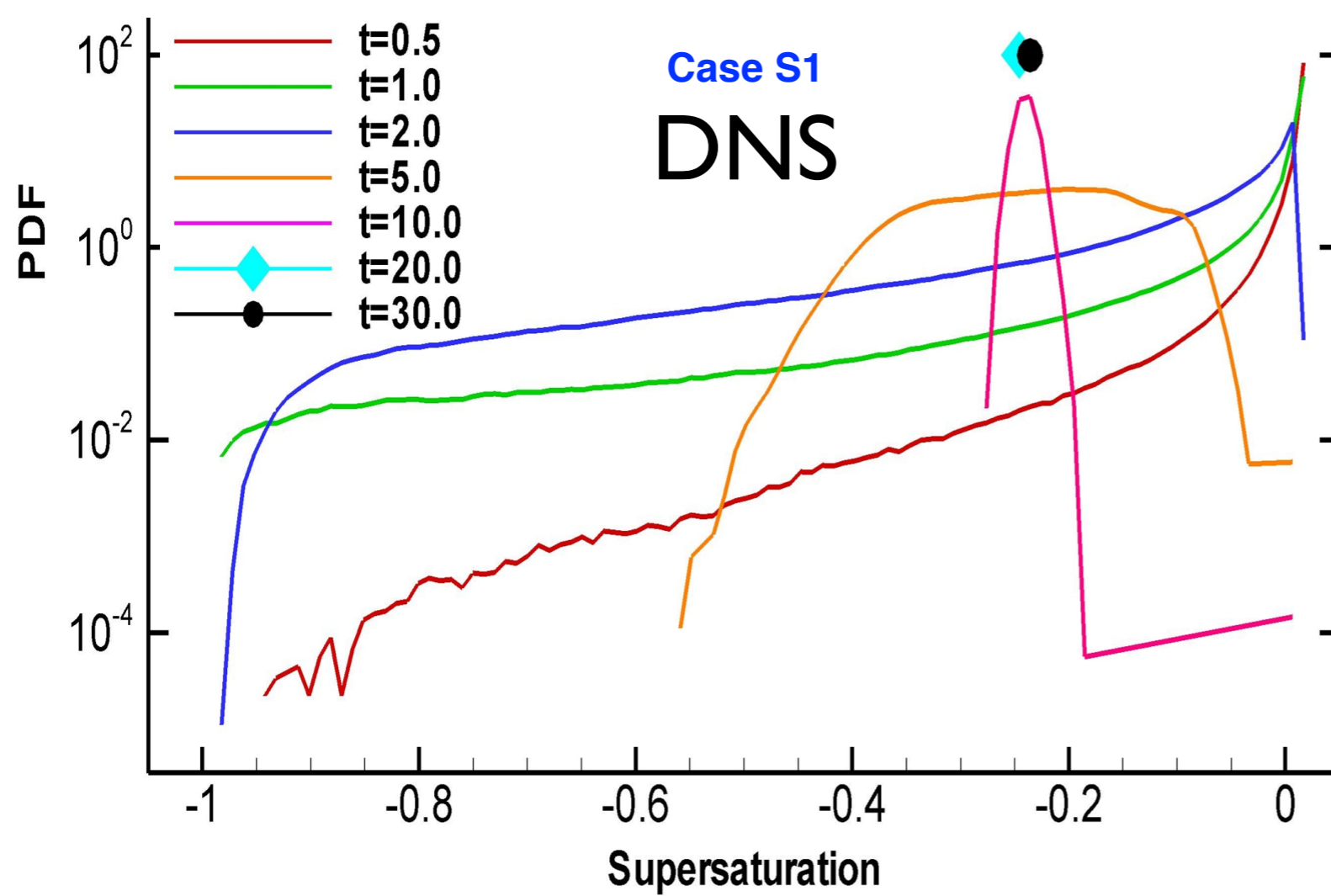
All droplets completely
evaporate by 30 s.

*Some droplets
grow initially in both.*

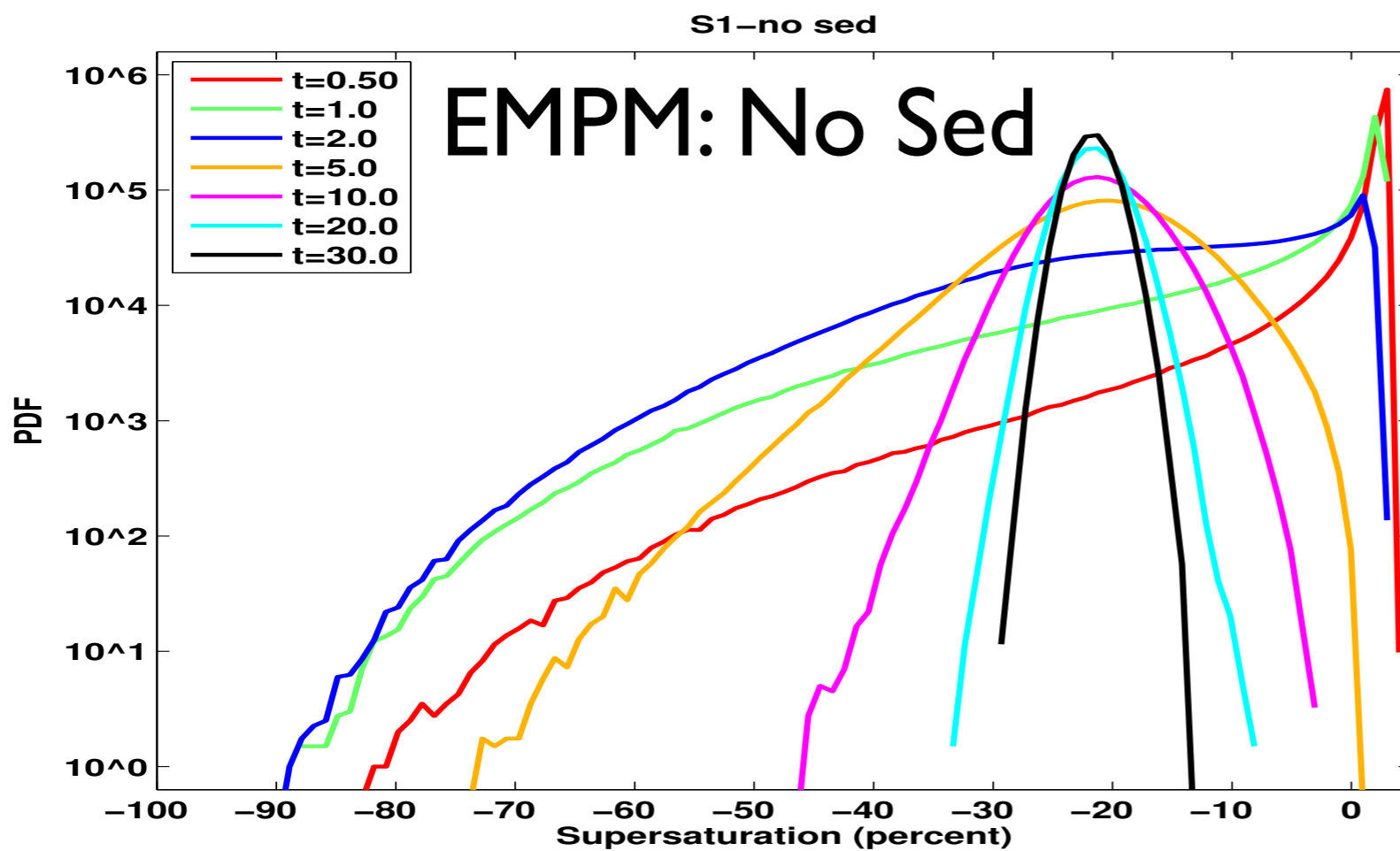


*In EMPM, droplets
evaporate faster than in
DNS to 2 s, then slower.*

**Wider DSD
at all times**



Super-saturation
at droplets
(including
completely
evaporated ones)



*Droplets encounter
less very dry air.*

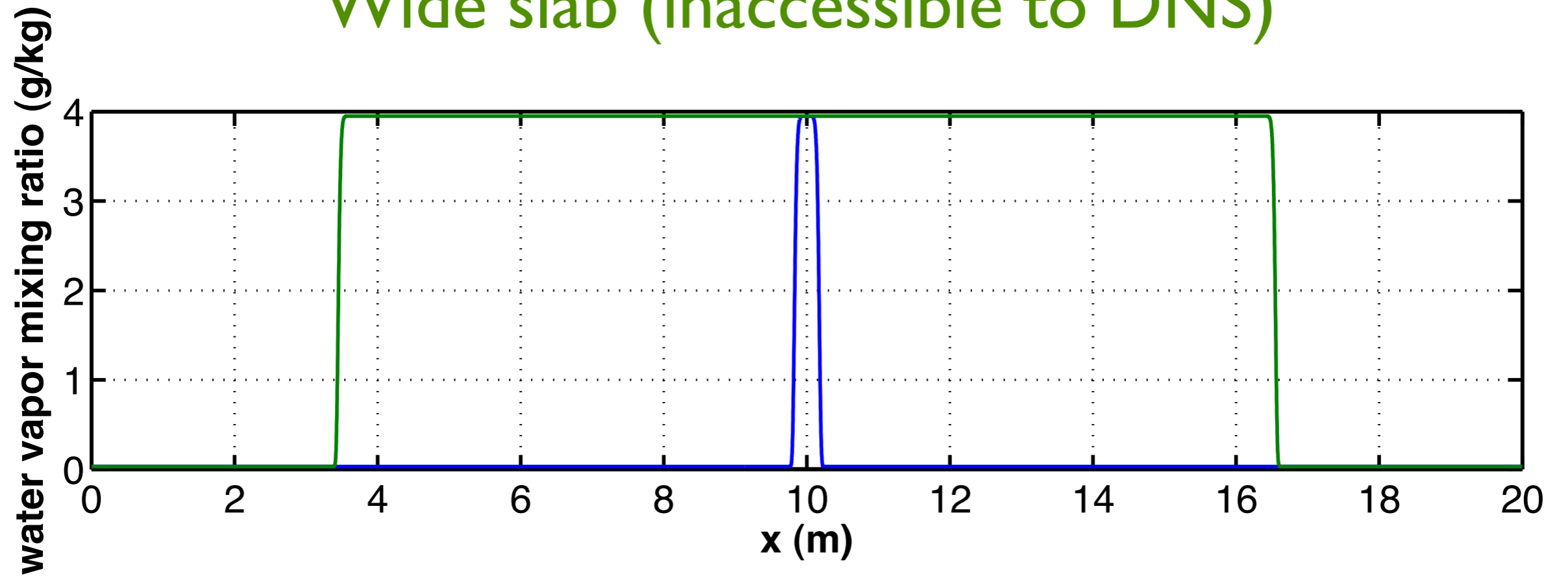
Slower mixing.

Example of EMPM results for larger scales not accessible to DNS.

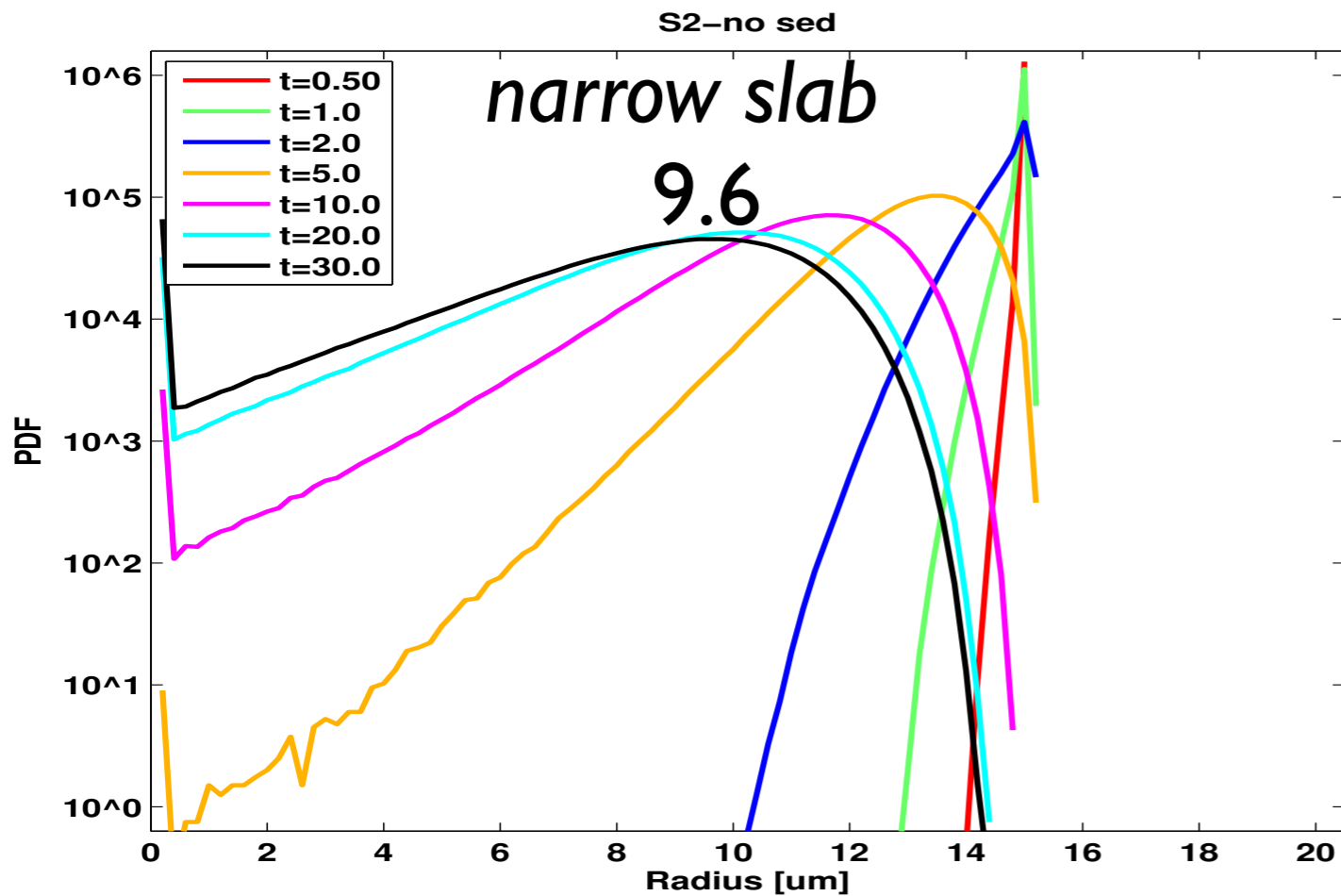
- DNS cost $\sim N^3$, EMPM $\sim N$.
- Example: Increasing domain size from 0.5 m to 10 m is an increase of $20^3 = 8000$ for DNS, but only 20 for EMPM.
- Due to the increased mixing time, there is an additional factor of $20^{(2/3)} \sim 7$, for a total increase of 56,000, versus 140 for the EMPM.

[EMPM DNS case for 20-m eddy size?]

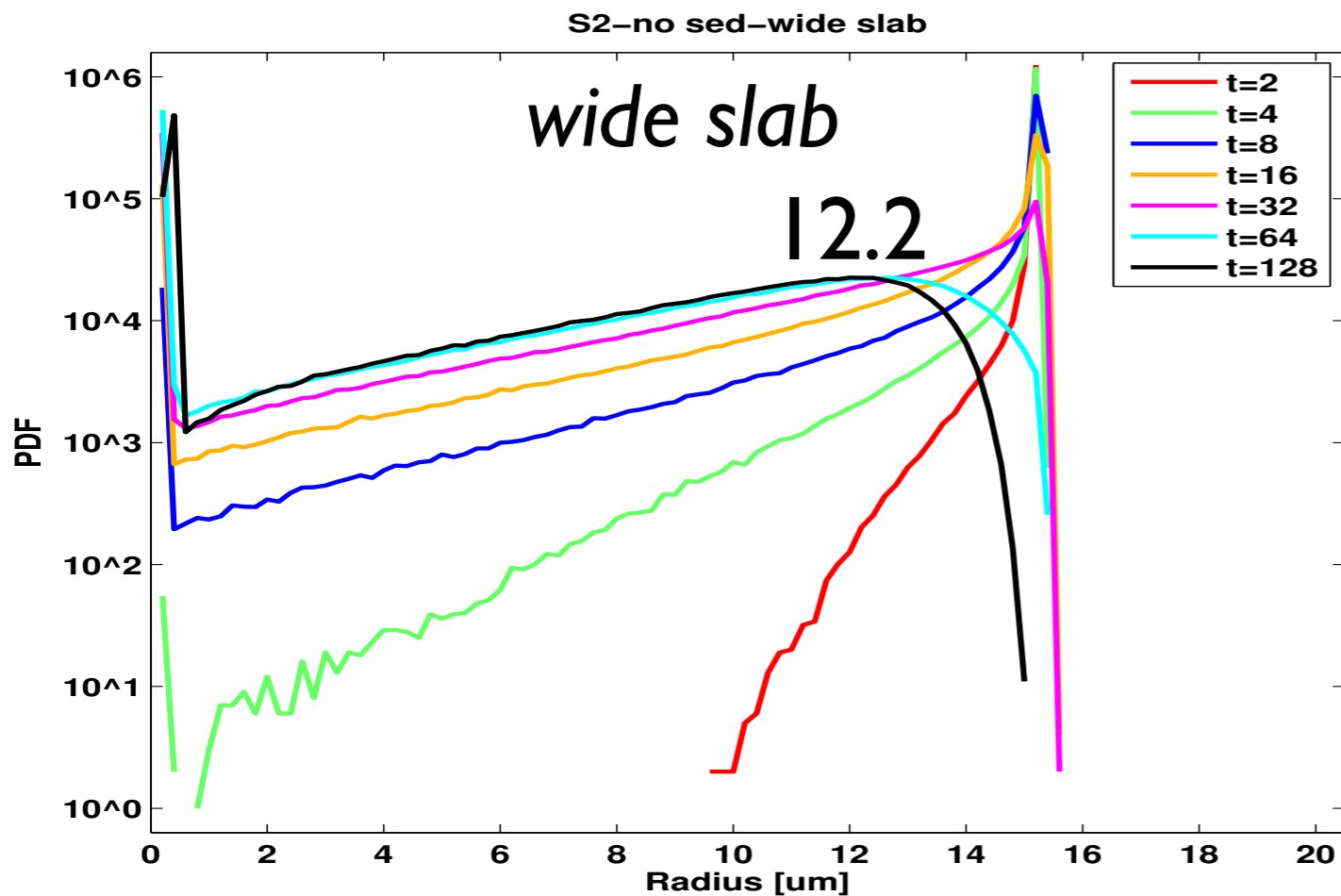
Wide slab (inaccessible to DNS)



Narrow slab (used in DNS)



Initial droplet radius is
15 microns.
Some droplets
completely evaporate.



Similar but slower
evolution.

Large droplet tail is
less eroded.