Droplet stochastic activation and spectrum broadening

in the presence of supersaturation fluctuations

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LES of cloud-scale flow

cloud updraft and interfacial instabilities (entraiment)



Microphysical variability

at sub-grid scales (SGS)

$$\blacktriangleright \ S = \langle S \rangle + S'$$

Mixing

Activation/deactivation

Super-droplets

LES grid box



Entraiment

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Stochastic activation

Köhler curve and potential

$$r\frac{\mathrm{d}r}{\mathrm{d}t} = D\left(S - \frac{A}{r} + \frac{B}{r^3}\right)$$
$$x \equiv r^2 \qquad S = \langle S \rangle + S'$$
$$\frac{\mathrm{d}x}{\mathrm{d}t} = -\frac{\partial V}{\partial x} + 2DS'$$

Abade, Grabowski and Pawlowska, JAS (2018)

Stochastic activation

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$$s_{\mathrm{eq}}(r)$$

$$s_{\mathrm{eq}}(r)$$

$$v_{\langle S \rangle}(r)$$

$$r_{\mathrm{d}}$$

$$r_{1} r_{\mathrm{c}}$$

$$r_{2}$$

$$r_{1}$$

Abade, Grabowski and Pawlowska, JAS (2018)

Stochastic activation

 $S=\langle S\rangle+S'$

Köhler potential

S_c S_c $S_{eq}(r)$ $S_{eq}(r)$ 0 0 haze droplet cloud droplet $0 < \langle S \rangle < S_c$ $V_{\langle S \rangle}(r)$ $V_{\langle S \rangle}(r)$ 0.1 $r_{\rm c}$ 1 10 $r_{\rm d}$ $r_1 r_c$ r_2 r [µm] r

Abade, Grabowski and Pawlowska, JAS (2018)

Feedback mechanism

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Supersaturation and velocity fluctuations



$$\frac{\mathrm{d}S_i'}{\mathrm{d}t} = -\frac{S_i'}{\tau_S} + aW_i'(t)$$

 $au_S-{
m condensation}$ and mixing

• Statistical model for W'(t)

Grabowski and Abade, JAS, 74 (2017)

Entraining cloud parcel

stochastic entrainment events



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Krueger et al., JAS, 54 (1997); Romps and Kuang, JAS, 67 (2010)

after a 1-km parcel rise



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after a 1-km parcel rise



after a 1-km parcel rise



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after a 1-km parcel rise



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- Prescribed flow u(r)
- Balance equations for entropy and water vapor
- Super-droplets

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$$\epsilon = 10^{-3} \text{ m}^2 \text{ s}^{-3}$$
 everywhere



- Prescribed flow u(r)
- Balance equations for entropy and water vapor
- Super-droplets

•
$$\epsilon = 10^{-3} \text{ m}^2 \text{ s}^{-3}$$
 everywhere

Droplet-size PDF



Droplet-size PDF



Droplet-size PDF



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Microphysical profiles

horizontally averaged



Summary and outlook

Simple model to mimic SGS variability

 Straightforward for super-droplets, difficult for bin microphysics

Important for rain development through collision/coalescence

Thermodynamic feedback: extends the distance of activation

Future: couple the SGS scheme with dynamic LES

Acknowledgements







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